# Volume function for character varieties 

Antonin Guilloux

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## 8-knot complement



The 8-knot complement $M_{8}$.

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The 8-knot complement $M_{8}$. Its fundamental group is $\Gamma_{8}=\left\langle a, b \mid a b^{3} a b^{-1} a^{-2} b^{-1}\right\rangle$.

## Peripheral torus



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The peripheral torus has a fundamental group $\mathbf{Z}^{2}$. There is an injection $\mathbf{Z}^{2} \rightarrow \Gamma_{8}$, whose image is generated by $m=a b$ and $I=a b a^{-1} b^{-1} a b^{-1} a^{-1} b$.

Triangulation of $M_{8}$

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$M_{8} \simeq$ gluing of the tetrahedra with vertex removed (2 tetrahedra, 4 faces, 2 edges, 1 'ideal vertex")

## Parametrization

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Take a complex parameter for each tetrahedron.

$z$

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There is a gluing equations :

$$
z^{2} w^{2} \frac{1}{(1-z)(1-w)}=1
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The deformation veriety

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