**Title**: Random expansions, infinite Bernoulli convolutions, and Local dimensions.

**Abstract**: For a certain class of algebraic bases  $\beta > 1$ , we consider the associated random  $\beta$ -transformation equipped with the unique measure  $\nu_{\beta}$  of maximal entropy. For a suitable metric, we study the local dimension of  $\nu_{\beta}$ . As a consequence, we are able to find the local dimension of the associated infinite Bernoulli convolution which can be seen as a marginal measure of  $\nu_{\beta}$ .