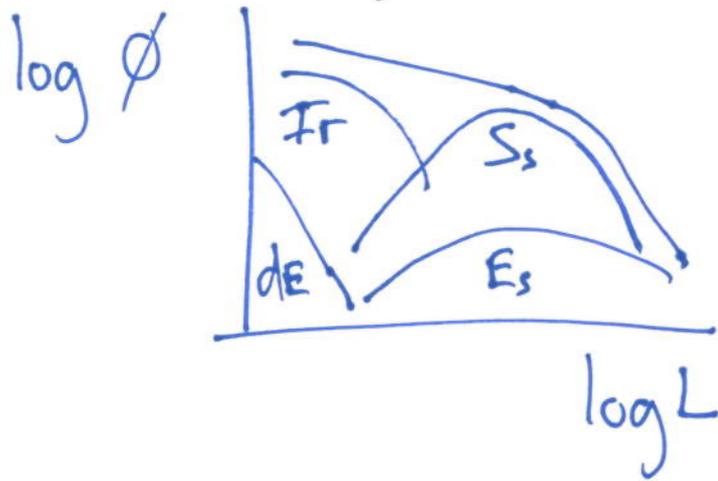


# Real luminosity functions for local universe

14.4.4



## Part 2 Spiral galaxies

Disc is blue (young) stellar population  $\equiv$  Population I

Bulge is red (old) stellar population  $\equiv$  Population II

Spiral arms have the bluest/youngest stars  
 $\Rightarrow$  site of current star formation.

due to gravitational collapse of gas compressed as it passes through the spiral arms, which are sound waves in the gas disc.

Discs are flattened by a factor  $\sim 10$

Vertical structure is also an exponential, so 3d structure of a spiral disc.

(in cylindrical polar co-ords)

14.45

$$\rho(R, z) = \rho_0 \exp\left(-\frac{R}{a}\right) \exp\left(-\frac{|z|}{h}\right)$$

↑ height above disc                      ↑ scale length                      ↑ scale height.

So typically  $h \sim \frac{a}{10} \sim \text{few } 100 \text{ pcs.}$

## Our Galaxy

Note: "our Galaxy" / "a galaxy"

→ 1<sup>st</sup> attempt to map our Galaxy by Herschel, 1785, by counting stars in different directions  
 ⇒ Sun close to centre; complex shape.

→ Star counts combined with distances from H-R diagram, still puts the Sun close to centre (650 pc from centre) with  $R \sim 10 \text{ kpc}$

→ Shapley, 1919 noted that all the globular clusters are on one side of sky (Kapteyn, 1922)

⇒ Sun not at centre of the Galaxy.

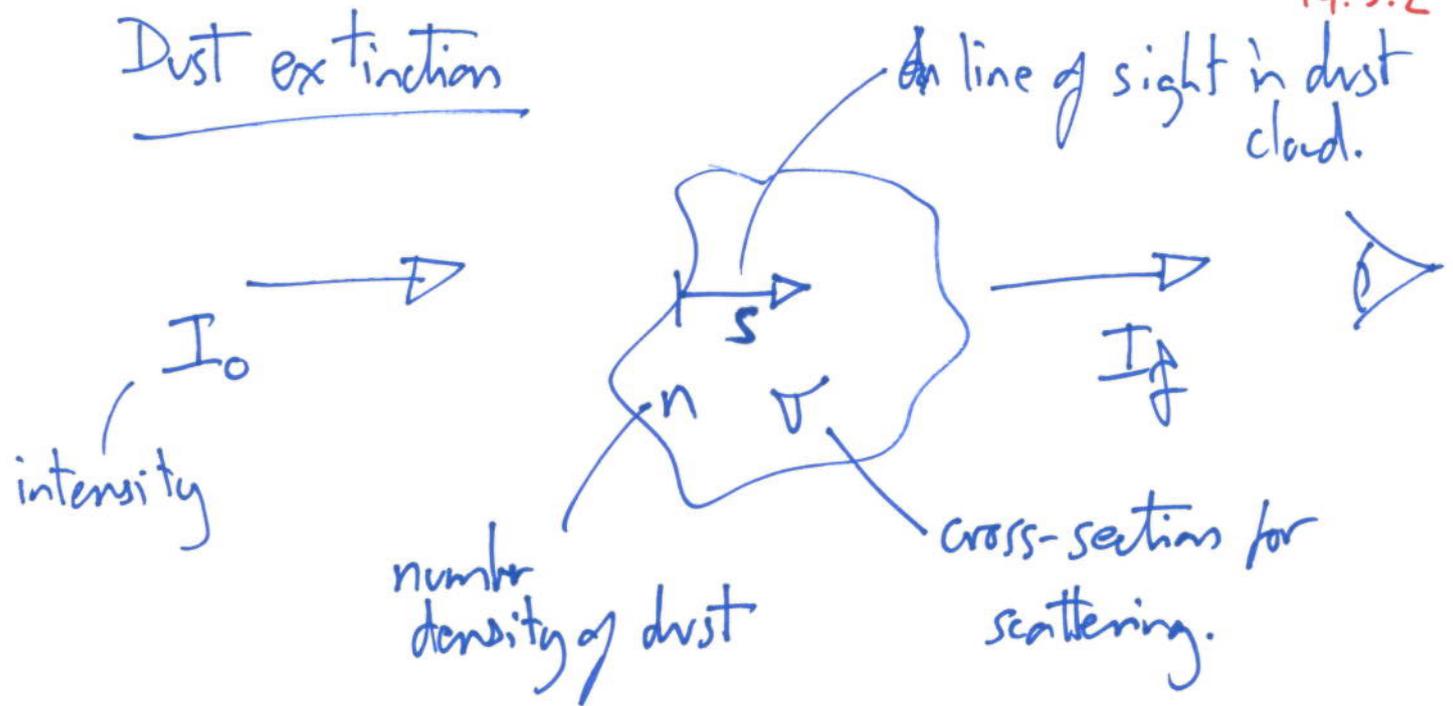
Distance scale from pulsating stars in globular clusters ⇒  $R \sim 100 \text{ kpc}$   $R_{\odot} \sim 20 \text{ kpc}$ .

Discrepancy due to dust extinctions in the interstellar medium (ISM)

→ caused Kapteyn to under-count distant stars.

→ caused Shapley to over-estimate distances to G.C.s due to extinctions to calibrator stars in the Galactic Plane.

Dust extinction



Fractional decrease in intensity.

$$\frac{dI}{I} = -n\sigma ds$$

Total effect by integrating.

$$\int_{I_0}^{I_f} \frac{dI}{I} = -\sigma \int_0^S n(s) ds$$

assume  $n = \text{constant}$

$$\Rightarrow I_f = I_0 \exp(-n\sigma s)$$

$\Rightarrow \tau \equiv \text{optical depth of cloud}$

Distance modulus

$$m - M = 5 \log_{10} \left( \frac{d}{10 \text{ pc}} \right) - A$$

$A$  dust extinction.

$$A = m_d - m_0 = -2.5 \log_{10} \left( \frac{I_d}{I_0} \right)$$

change in apparent  
mag. due to extinction

$$= -2.5 \log_{10} (e^{-\tau})$$

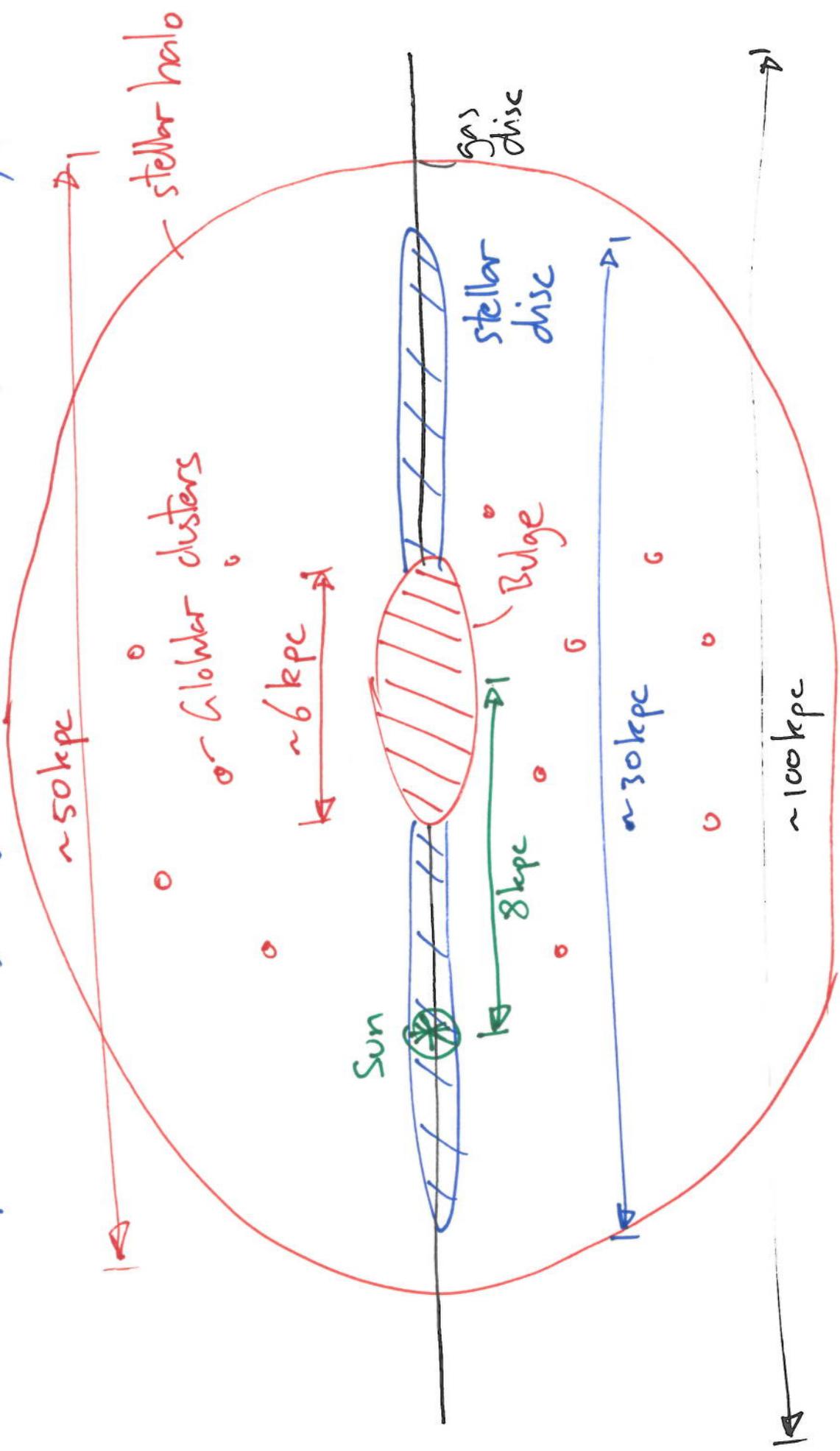
$$= \underline{\underline{1.09 \tau}}$$

useful to remember  $A \approx \tau$

Typically in Galactic plane  $A \approx 1 \text{ mag/kpc}$

In practice dust extinction can be estimated by the  $\lambda$ -dependence of the cross-section. (dust extinction is often called reddening)

structure of the milky way based on star counts, accounting for extinction.



# Stellar components

Population I: thin disc,  $h \sim 300 \text{ pc}$   
 $a \sim 2 \text{ kpc}$

Note:  $h$  is different for different spectral types.

K stars,  $h \sim 350 \text{ pc}$

A " ,  $h \sim 200 \text{ pc}$

OB " ,  $h \sim 100 \text{ pc}$

hotter  
 & more  
 massive  
 & less  
 & younger

$\Rightarrow$  short-lived stars found closer to Galactic Plane  $\Rightarrow$  stars form in G.P.,  
 move to higher average scale heights as  
 their orbits evolve through scattering with  
 other stars.

Population II:

$\rightarrow$  Galactic / ~~stellar~~ stellar halo  
 $\sim$  spherical,  $\rho \propto R^{-3}$

mainly v. old stars

very low metallicity  $\ll 10^{-2}$  Solar

fraction of material not H or He

stars form from the ISM, which initially is only H & He, but is polluted over time by heavier elements formed in stars & returned to ISM by when stars die.

So metallicity depends on the star formation history of the region of formation.

→ G. halo is now thought to be debris from dwarf galaxies that have been tidally disrupted and accreted by the Milky Way.

### Galactic edge:

→ Globular clusters, v. old stars  $\approx 12$  Gyrs from modeling the H-R diagram for each cluster. (cf. Universe  $\sim 13.7$  Gyr old).  
metallicity  $\sim 10^{-2}$  Solar.

→ G.C.s thought to have formed early in the history of the M.W. - early in the gravitational collapse of the primordial gas cloud.

→ Galactic bulge: v. old stars. metallicity  $\approx 0.5$  Solar

Also,  $h \sim 400 \text{ pc}$  (still a disc-like/flattened object, unlike the Halo/dista of G.C.s).

→ indication of intense star formation in the centre of the early galaxy (with SNe polluting the ISM).

→ thick disc: old stars with  $h \sim 1350 \text{ pc}$   
controversial whether this is part of the disc or a flattened part of the halo.

By stellar mass: thin disc  $\sim 10^{11} M_{\odot}$   
Bulge  $\sim 10^{10} M_{\odot}$   
Halo  $\sim 10^9 M_{\odot}$  } by modelling the luminosity & colour of the stellar population.

By numbers in the Solar neighbourhood:

$\sim 98\%$  thin disc

$\sim 2\%$  thick disc

$\sim 0.1\%$  halo

Sun is at  $z \approx 15 \text{ pc}$

⬆ height above Galactic Plane.

$V_z = 7 \text{ km s}^{-1}$  toward North Galactic Pole.

## Non-stellar components

→ gas } ISM      By mass H ~ 70%  
 → dust }            28% He  
 → dark matter      2% metals.

H gas exists in 3 forms:

molecular,  $H_2$

~~atomic~~ Atomic, HI

ionised, HII

HII is the most visible because it emits strong recombination emission lines

⇒ dominates the line emission of galaxies.

Ionisation potential of H is  $13.6 \text{ eV} \approx 2.2 \times 10^{-18} \text{ J}$

so to photoionise, we need photons of

$$\lambda \leq \frac{hc}{2 \times 10^{-18} \text{ J}} = 91 \text{ nm.}$$

↗ far ultraviolet.

Recall, Wien displacement law for B.B. emission,

$$\lambda_p T = 0.0029 \text{ m K}$$

↑ peak  $\lambda$  of B.B.

set  $\lambda = 91\text{nm} \Rightarrow T \sim 30,000\text{K}$

14.6.4

so only the hottest stars can produce large quantities of photons to ionise the ISM.

So only see HII regions around the hottest, youngest stars (OB stars)

$\Rightarrow$  emission lines are a powerful tracer of current star formations.

Studies at low  $z$  show where stars form in galaxies (in spiral arms)

Studies at high  $z$  attempt to trace the star formation history of the Universe.

size of an HII region by assuming eqm between ionisation & recombination

$$N \approx \frac{L_{UV}}{13.6\text{eV}} = \frac{4}{3} \pi r_s^3 n_e n_p \alpha$$

$\uparrow$  ionisation rate                       $\uparrow$  volume of HII region                       $\uparrow$  recomb. coeff. / number densities of  $e^- p^+$

assume  $n_e = n_p = n_H$

$$\Rightarrow r_s = \left( \frac{3N}{4\pi\alpha} \right)^{1/3} n_H^{-2/3}$$

$\uparrow$   $\rightarrow$  measure  $n_H$  from HII   
 $\approx$  few pc around

Strömgren radius

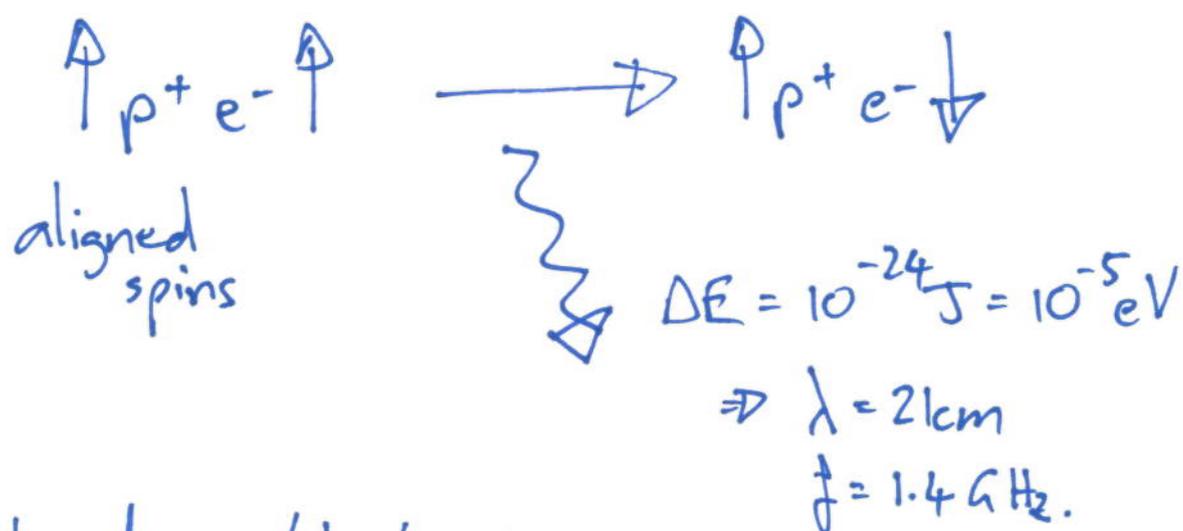
an OB star.  
14.6.5

H I has high excitation potential,

$$n=1 \rightarrow n=2 \text{ is } 10\text{eV}$$

so we don't see emission lines, except in H II regions.

Fortunately H I has a unique transition in the radio spectrum, due to hyper-fine splitting of ground state,



Extremely useful for tracing H I gas, because collisionally excited even at v. low temperatures.

$$\Delta E \approx \overline{\text{K.E.}} = \frac{3}{2} kT$$

$\Rightarrow T \geq 0.05\text{K}$  is sufficient.

Typically ISM,  $T \sim 100\text{K}$ , whole universe  $\sim 3\text{K}$   
 $\Rightarrow 21\text{cm}$  line emitted by all the H I in Universe!

mapping the 21cm line in m.w. & nearby galaxies

- ⇒ HI confined to disc of spirals,  $h \sim 100 \text{ pc}$
- ⇒ Extends well beyond the stellar disc
- ⇒ almost entirely absent in bulge and in elliptical galaxies.

Believed the galaxies accrete HI gas from the intergalactic medium (IGM), infall into the centre of galaxies is halted by cons. of ang. momentum, disc is the with circular orbits is lowest energy configuration for specific ang. mom. distr.

Another v. useful feature is that 21cm transition is highly forbidden,  $\Rightarrow \tau = 4 \times 10^{14} \text{ s}$   
 $\approx 10 \text{ million years!}$   
 timescale for deexcitation.

- ⇒ emission is v. weak, but absorption also weak  $\Rightarrow$  most of m.w. is transparent.
- ⇒ map m.w. structure.

Also allows us to measure total mass in HI

$\approx 10^{10} M_{\odot}$   
 $\approx 10\%$  stellar  
 mass of the  
 disc.

but  $\bar{n}_H = \frac{N_{\text{tot}}}{\text{Volume}} = \frac{10^{10} M_{\odot} / m_H}{\pi R^2 h}$

mean number  
density of H

Take  $R \sim 30 \text{ kpc}$ ,  $h \sim 100 \text{ pc}$   
 $\Rightarrow \bar{n}_H \approx 1 \text{ cm}^{-3}$

$\text{H}_2$  is almost impossible to detect, lack of emission transitions.

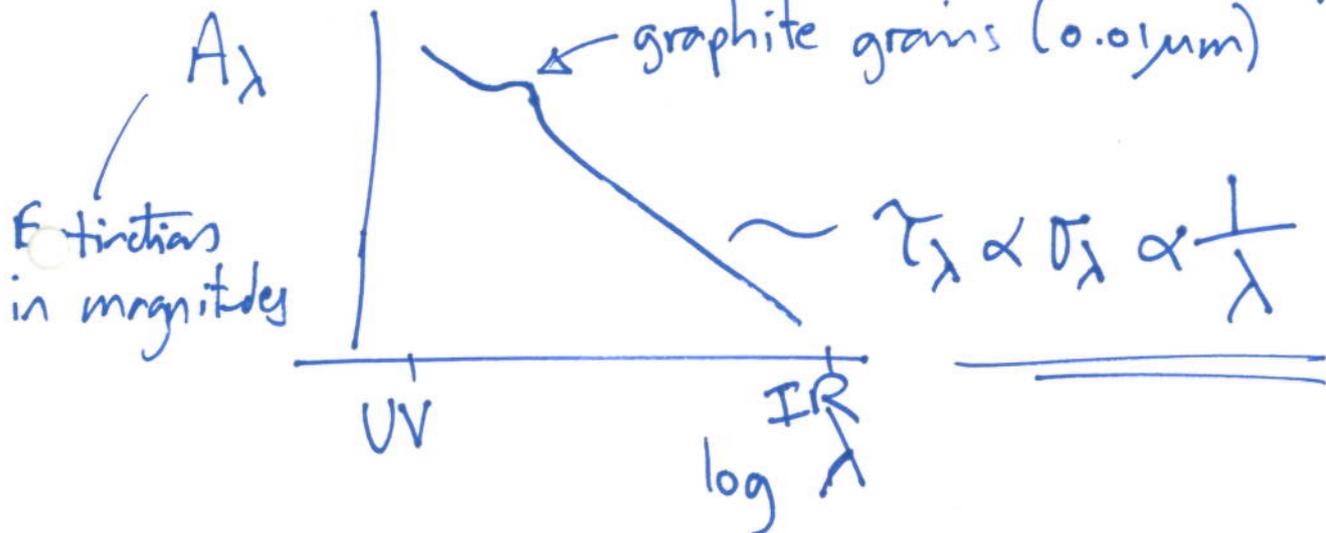
In practice molecular gas is traced by via the vibrational transitions of asymmetric molecules esp. CO, which is relatively abundant, & has transitions at  $\lambda = 1.3 \text{ mm}$  &  $2.6 \text{ mm}$ .

Mapping results  $\Rightarrow$  mol. gas confined to small, cold, dense regions in disc  $\rightarrow$  molecular clouds typically  $R \sim 10-100 \text{ pc}$ ,  $\rho \sim 10^3$  typical ISM.

Grav. collapse of mol. clouds in spiral arm density waves that forms stars.

→ find HII regions form at margins of mol. clouds, e.g. Orion nebula.

Dust Extinction is stronger in blue than red.



This slope across UV-optical-IR is characteristic of scattering, specifically Mie scattering, occurs when  $R_g \approx \lambda$

$\Rightarrow$  dust scattering.  $R_g$  grain size

$R_g \approx 0.01 - 1 \mu\text{m} \approx$  smoke particles

cf  $R_g \gg \lambda \Rightarrow \tau$  independent of  $\lambda$

$R_g \ll \lambda \Rightarrow$  Rayleigh scattering.  $\tau \propto \frac{1}{\lambda^4}$

molecular absorption features from detailed spectroscopy <sup>14.7.5</sup>

→ mostly silicates (rock)

→ often coated in ices of volatiles, (eg.  $H_2O$ ,  $CO$ ,  $NH_3$ ,  $CH_4$ ).

---

14.8.0

Dust condenses in cold dense environments

→ molecular clouds

→ outflows from red giant stars.

Note: because of reddening by dust, it is best to use IR for studies of galaxy structure.

At larger  $\lambda$ 's in mid-to-far IR the dust is seen in emission, heated by surrounding stars.

## Star formation rate indicators

1) UV light from young massive stars  
(seen in the optical & IR at high  $z$ ).

2) Emission lines from HII regions, (powered also by the UV emission of young stars).

At low  $z$ , we see because reprocessing UV light into visible light.

At high  $z$ , can detect the v. strong Ly $\alpha$  line ( $n=2 \rightarrow n=1$ ) even when the star light continuum is undetectable.

3) Strong far-IR emission from dust heated by obscured massive stars

seen even when the star formation regions are completely hidden by dust.

recall,  $L_{\text{BB}} = A \sigma T^4$

↑ luminosity high because area of dust grains is high.

Studies of star formation show a small fraction of galaxies w. v. high star formation rates  $\Rightarrow$  distinct episodes of star formation in the history of ~~ex~~ each galaxy.

2 types of star forming galaxies:

$\rightarrow$  Starburst galaxies

- galaxies with strong 1) + 2).

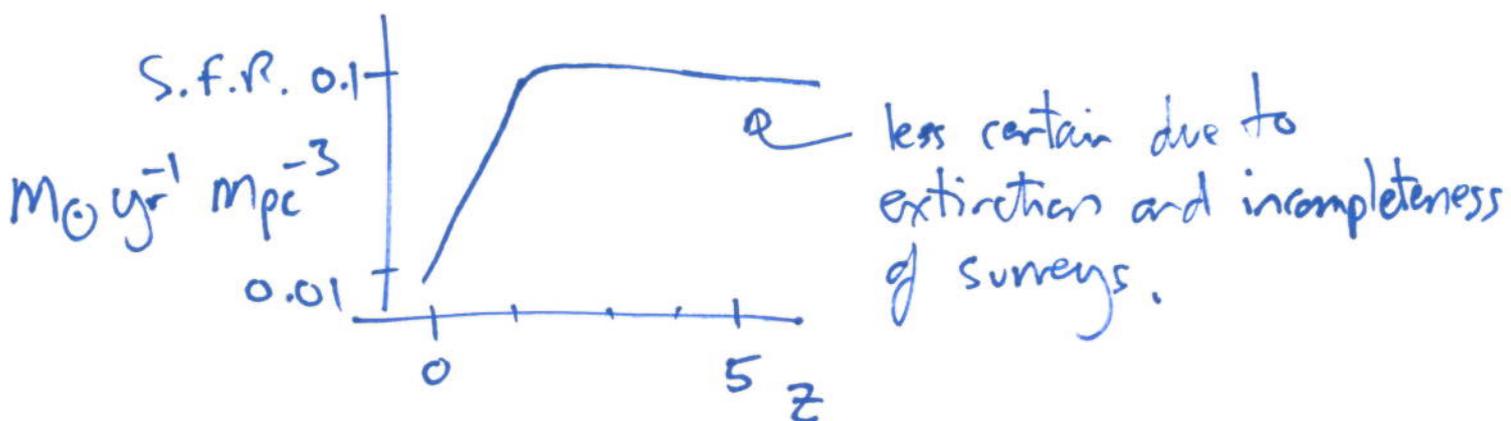
$\Rightarrow$  un-obscured star formation

$\rightarrow$  Ultra-luminous infra-red galaxies

ULIRGs

- galaxies w. strong 3).

Galaxy surveys trace star formation over cosmic history  $\Rightarrow$  Madau plot.



Crucial input to galaxy formation models.

## Kinematics of spiral galaxies

How do the stars orbit?

→ in a disc. in a coherent rotation?  
or random directions? or highly eccentric?

Use Doppler effect to probe kinematics,  
measure the radial velocity vs radius  
( $V_r$  - component of velocity along  
our line of sight.)

Recall 
$$\frac{\Delta\lambda}{\lambda} \approx \frac{V_r}{c}$$

need to correct velocity for the inclination  
of the galaxy.



estimate  $i$  by assuming disc is circular  
and comparing semi-major & semi-minor  
axes  
i.e.  $b = a \cos i$

Use long-slit spectroscopy to measure the Doppler shift of emission lines from HII regions in disc, along the semi-major axis.

Results  $\Rightarrow$  disc does rotate coherently, systematic shift from one side of the galaxy to the other.

$\Rightarrow$  bulge shows broadening of absorption lines from the many stars,  
 $\Rightarrow$  stars orbits are randomly orientated.

Useful to think of stars as particles in collisionless gas.

Disc  $\Rightarrow$  cold gas, supported against gravity by rotation.

Bulge  $\Rightarrow$  hot gas, pressure supported against gravity.

---

Can use rotational velocities to measure mass of galaxy.

cf. Solar system - circular orbits around a point mass.

equate centripetal force & grav. force.

planet mass  $m_p$       mass of sun  $M_\odot$

$$\frac{m_p v^2}{r} = \frac{G M_\odot m_p}{r^2}$$

orbital separation  $r$

$$\Rightarrow M_\odot = \frac{v^2 r}{G}$$

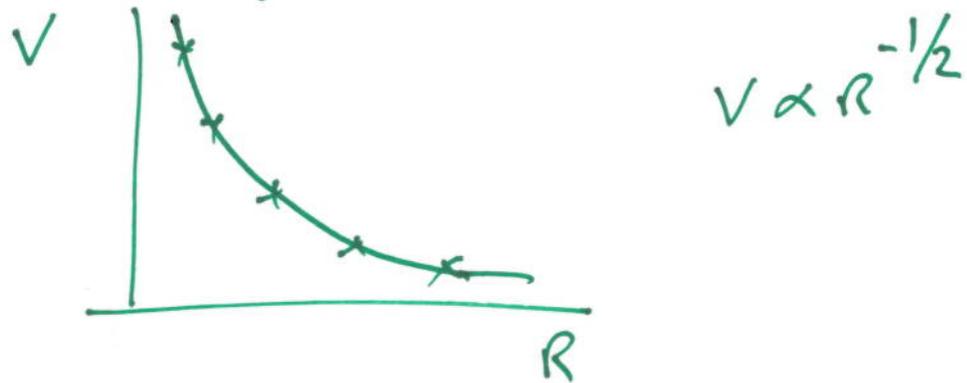
For Earth,  $v = \frac{2\pi \text{ 1 AU}}{1 \text{ yr}} = 30 \text{ km s}^{-1}$

$$\Rightarrow M_\odot = 2 \times 10^{30} \text{ kg.}$$


---

Recall,  $M_{\odot} = \frac{v^2 R}{G}$

Rotation curve of Solar system.



Galaxies more complex because mass is not concentrated at the centre,

But Gauss's Theorem, general property of vector fields.

$$\underbrace{\int_S \underline{F} \cdot d\underline{s}}_{\text{surface integral of field}} = \underbrace{\int_V \underline{\nabla} \cdot \underline{F} \, dV}_{\text{volume integral of divergence of field.}}$$

For, gravitational field divergence is mass.

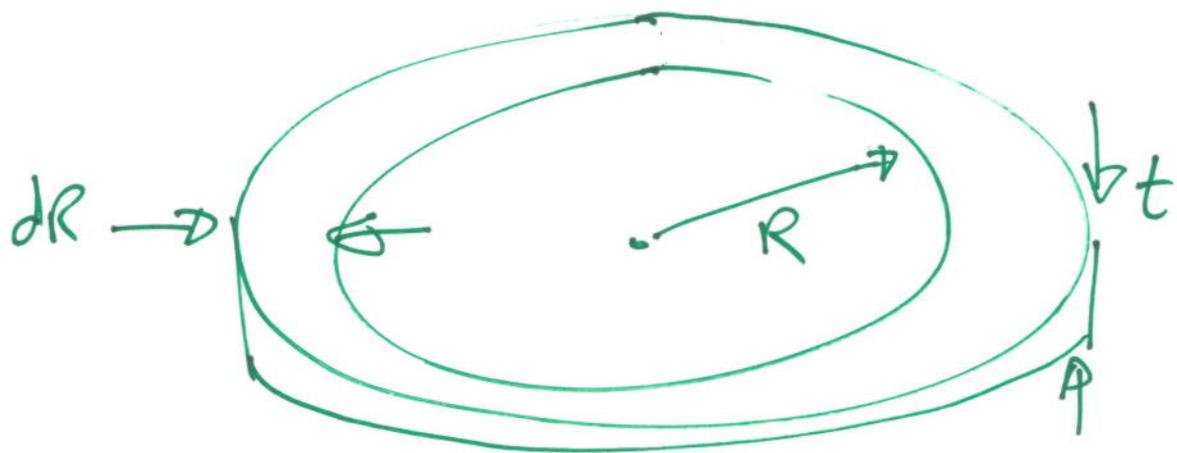
$$\Rightarrow M(<R) = \frac{v^2 R}{G}$$

mass enclosed by the orbit.

only strictly true for spherically symmetric mass distn.

consider  $\rho(r)$ , by assuming a 3D mass distn.

① assume all mass in the disc



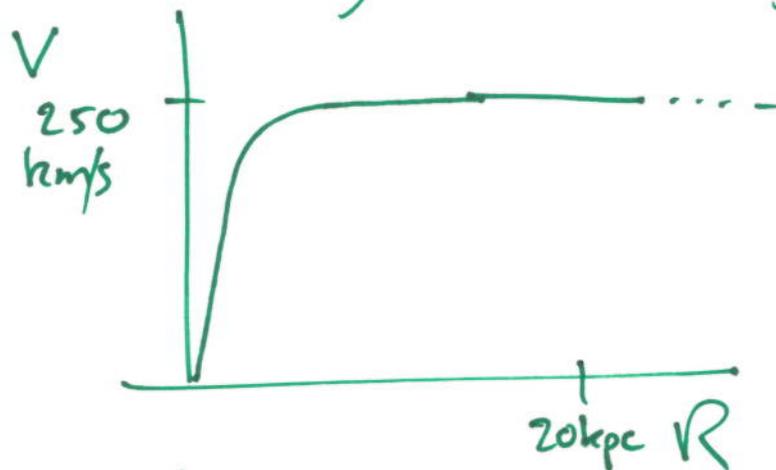
Volume of annulus,  $dV = 2\pi R t dR$

mass of annulus,  $dM = \rho 2\pi R t dR$

$$\Rightarrow \frac{dM}{dR} = 2\pi R t \rho = \frac{v^2}{G}$$

$$\Rightarrow \rho(r) = \frac{v(r)^2}{2\pi t R G} \propto \frac{1}{R}$$

14.9.3  
 Observed rotation curves of spiral galaxies rise steeply in centre, as more mass is enclosed, then stay flat to large radii



(should have done this before  $\rho(r)$ , and talked about  $\rho(r)$  or  $M(r)$ .)

If mass is all in disc (which is expected if stars dominate mass), then  $\rho(r) \propto \frac{1}{R}$

Recall, the brightness profile of galaxy discs  $\propto e^{(-R/a)}$

which traces the stars.

$\Rightarrow$  stars do not account for the dominant mass of a galaxy.

$\Rightarrow$  galaxies dominated by Dark Matter!

For a typical spiral galaxy,  $V \sim 250 \text{ km s}^{-1}$  at  $R \sim 20 \text{ kpc}$  14.9.4

$$\Rightarrow M(< 20 \text{ kpc}) = 6 \times 10^{41} \text{ kg.} \\ = 3 \times 10^{11} M_{\odot}.$$

---

Consider mass to light ratio:  $\frac{\text{Mass}}{\text{Luminosity}} \frac{M_{\odot}}{L_{\odot}}$

typically for discs of spirals.

$$\frac{M}{L} \sim 5 \frac{M_{\odot}}{L_{\odot}}$$

measurements at largest radii, e.g. from the orbits of dwarf galaxies

$$\frac{M}{L} \sim 50 !$$

---

② Exercise: show that spherically distributed mass must have density profile of

$$\rho(r) = \frac{v^2}{4\pi G R^2} \propto \frac{1}{R^2}$$

## Kinematics of the Milky Way.

Difficult to measure from our location within the galaxy, and due to dust extinction.

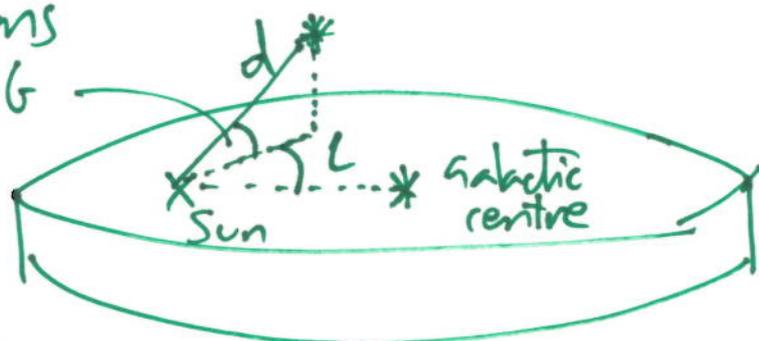
But for nearby stars we can measure the 3D velocity,

$v_r$  from Doppler shift

also  $v_t$ , transverse velocity from proper motion, which is the angular velocity on the sky.

$$\mu = \frac{d\theta}{dt} = \frac{v_t}{d}$$

positions

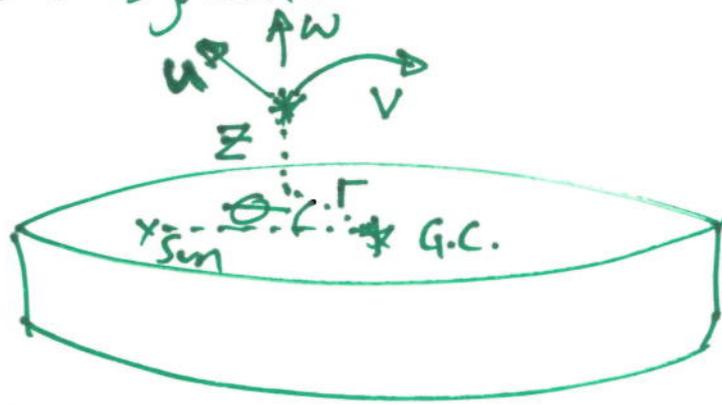


Galactic co-ordinates.

$l \equiv$  Galactic longitude,  $b \equiv$  Galactic latitude  
 $d =$  distance. — includes all of the uncertainties

For kinematics, easier to use a Galaxy-centred co-ordinate system.

14.9.6 + 14.10.0



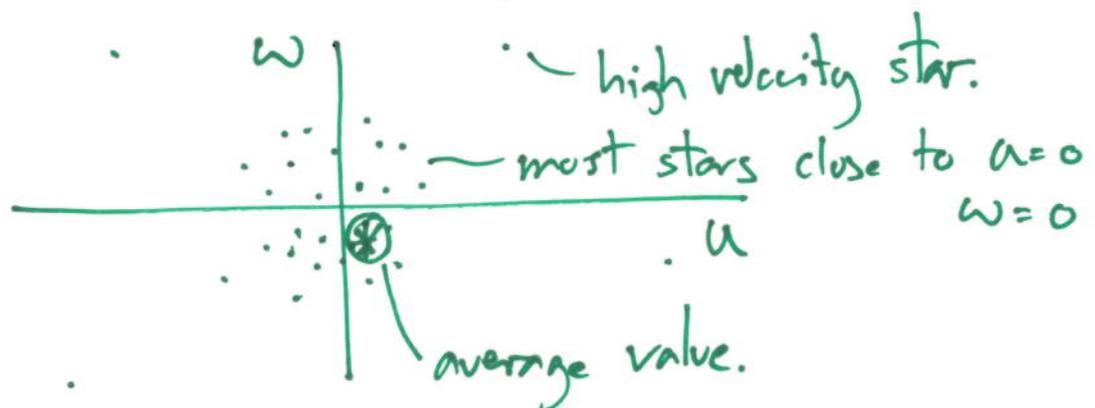
position  $(r, \theta, z)$

velocity  $(u, v, w)$  measured wrt the local standard of rest, which is an idealised Solar orbit.

(orbit the Sun would have, if perfectly circular & in the plane of the galaxy.)

14.10.0

For v. nearby stars can measure 3D velocity, so we know  $u, v, w$  wrt the LSR.



Assume the Galaxy is stable

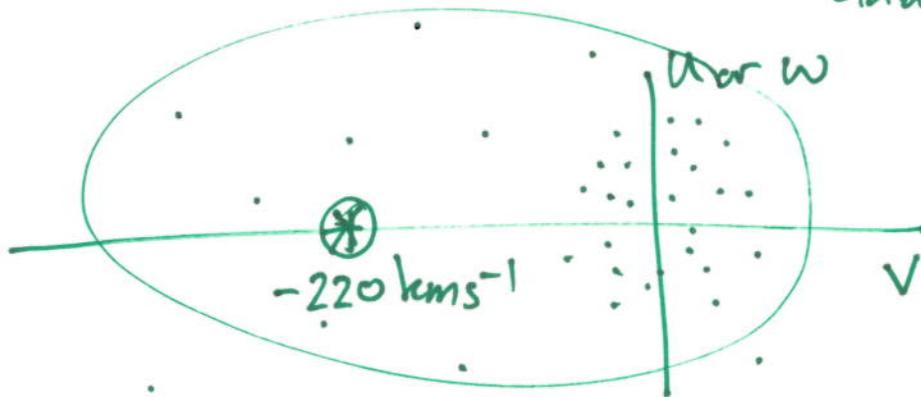
14.10.1

$$\Rightarrow u_{\odot} = -\bar{u} = -9 \text{ km s}^{-1}$$

$$w_{\odot} = -\bar{w} = 7 \text{ km s}^{-1}$$

we are moving towards Gal. Centre

towards North Galactic pde.



↳ high velocity stars

High velocity stars are halo stars passing through the disc, not orbiting the Galaxy with the disc. Assume halo has negligible net rotation

$$-\bar{V}_{\text{halo}} = V_{\text{LSR}} = 220 \text{ km s}^{-1}$$

Recall,  $M(<R) = \frac{V^2 R}{G}$

$$V_{\odot} \approx 220 \text{ km s}^{-1}$$

$$R_{\odot} \approx 8 \text{ kpc}$$

e.g. by measuring the average distance to globular clusters.

↑ distance of Sun from G.C.

$$\Rightarrow M_{\text{MW}}(<R_{\odot}) = 1.7 \times 10^{41} \text{ kg} \\ = \underline{9 \times 10^{10} M_{\odot}}$$

Note

$$P_{\odot} = \frac{2\pi R_{\odot}}{V_{\odot}} = \underline{220 \text{ Myr.}}$$

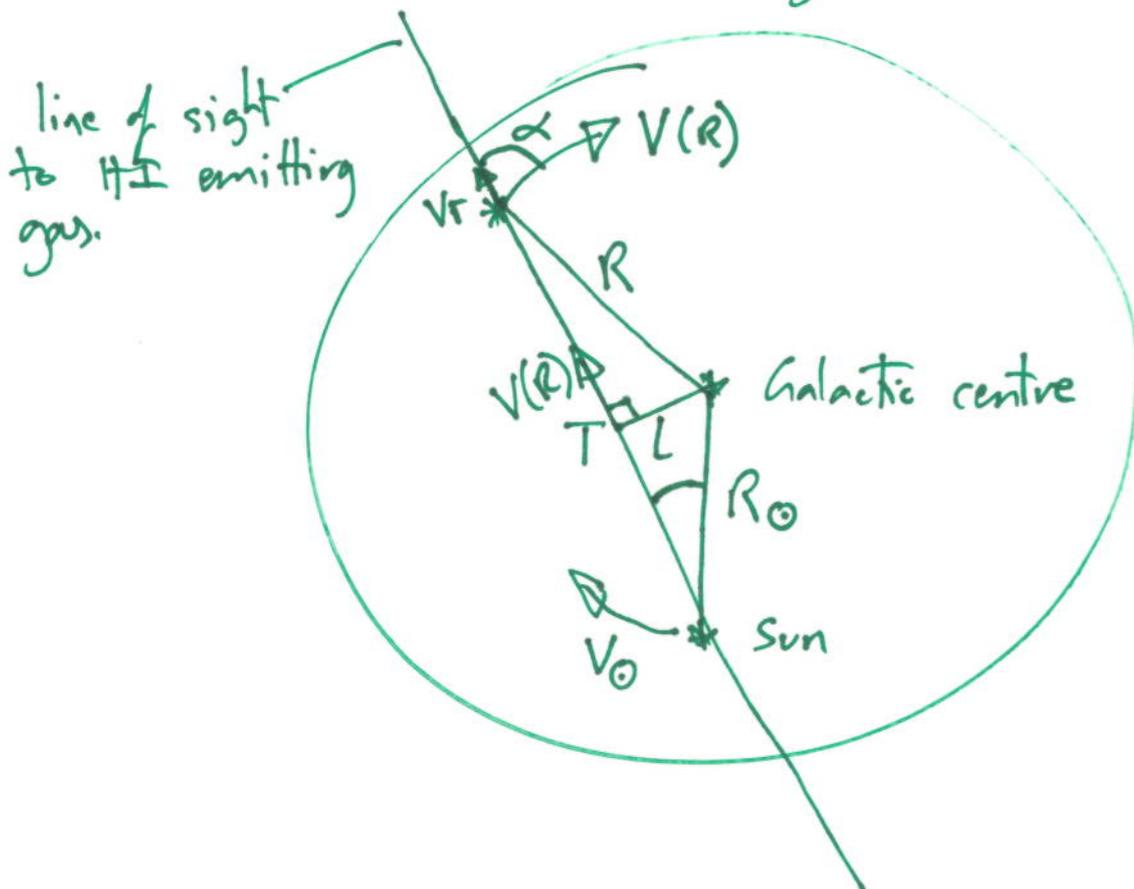
14.10.2

We want to measure the rotation curve of the Milky Way.

→ need velocities at large distances

⇒  $V_r$  but not  $V_t$

→ also need to see through the dust in the Galactic plane. ⇒ use the 21cm of HI. Doppler shift of line →  $V_r$  also visible at large distances.



$$V_r = \underbrace{V(R) \cos \alpha}_{\substack{\text{component of} \\ \text{gas cloud velocity} \\ \text{along our line of} \\ \text{sight.}}} - \underbrace{V(R_0) \cos(90-L)}_{\substack{\text{Component of our} \\ \text{own velocity along} \\ \text{our line of sight.}}}$$

measured radial velocity

Know everything except  $V(R)$  and  $\alpha$ , which depends on  $R$ .

Trick, assume the maximum  $V_r$  measured is at the tangent point, where  $V_r = V(R)$

Reasonable assumption, mainly because at that point all of  $V(R)$  is along our line of sight (so  $V_r$  has a maximum).

$$V_r = V(R) - V(R_0) \cos(90-L)$$

$\uparrow$   
 $R_0 \sin L$

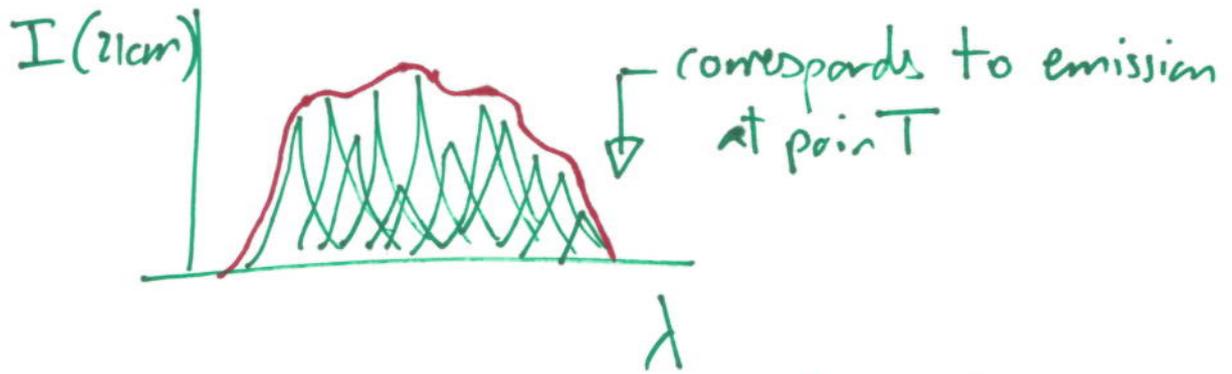
$$\Rightarrow V(R_0 \sin L) = V_{r, \text{max}} + V(R_0) \sin L$$

$\uparrow$   
maximum measured radial velocity.

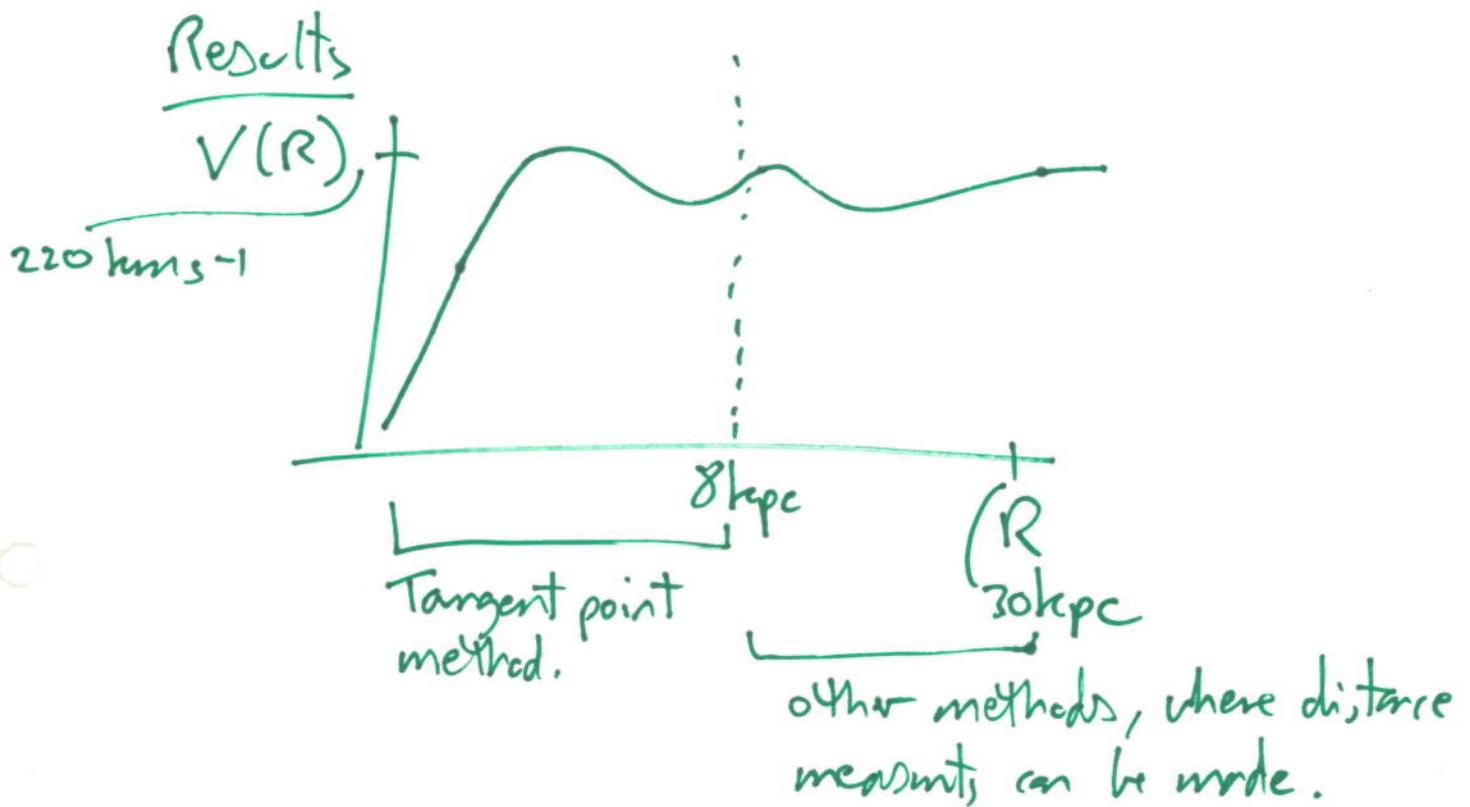
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# Example spectrum at one $L$

14.10.4



By measuring at different  $L$ 's we get  $V(R)$  for different tangent points, and build up the rotation curve of our Galaxy.



$\Rightarrow$  M.W. is also dominated by dark matter!

(recall, density of stars drops off exponentially with a scale length of  $\sim 2 \text{ kpc}$ .)

$$M_{\text{MW}} (< 20 \text{ kpc}) \approx 2 \times 10^{11} M_{\odot}$$

Using orbits of dwarf galaxies, orbiting the M.W.

$$\Rightarrow M_{\text{MW}} \geq 10^{12} M_{\odot}$$


---

$$\frac{M}{L} \approx 5 \text{ within the stellar disc } \left( \frac{M_{\odot}}{L_{\odot}} \right)$$

$\approx 50$  to edge of detectable disc.

$\approx 100$  at orbits of dwarf galaxies.

---

What is dark matter?

It isn't : normal stars

dust (would be seen by extinction).

gas ( " " " " e.g. HI 21cm line, or CO lines).

2 main candidates:

MACHOs : massive compact halo objects.

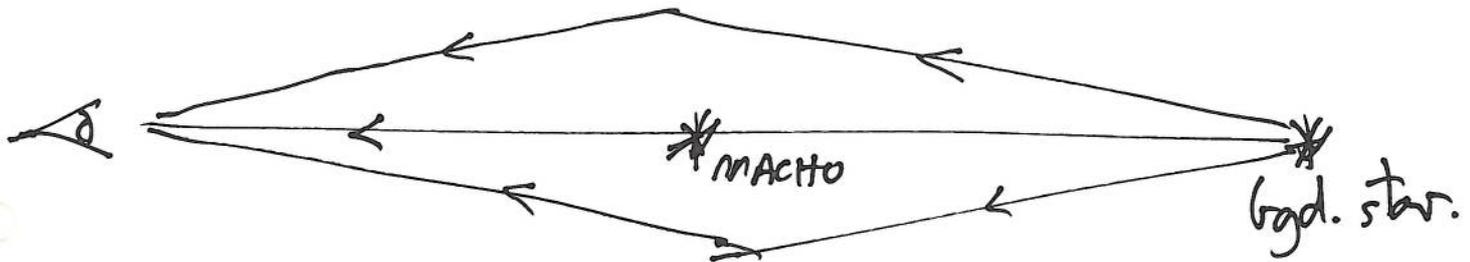
- normal baryonic matter, e.g. planets, brown dwarfs, white dwarf stars, Black holes.

WIMPs : weakly interacting massive particles

14.11.2  
- exotic particle, with mass, but which interacts weakly w normal matter.  
(e.g. neutrinos).

↳ net neutrinos!

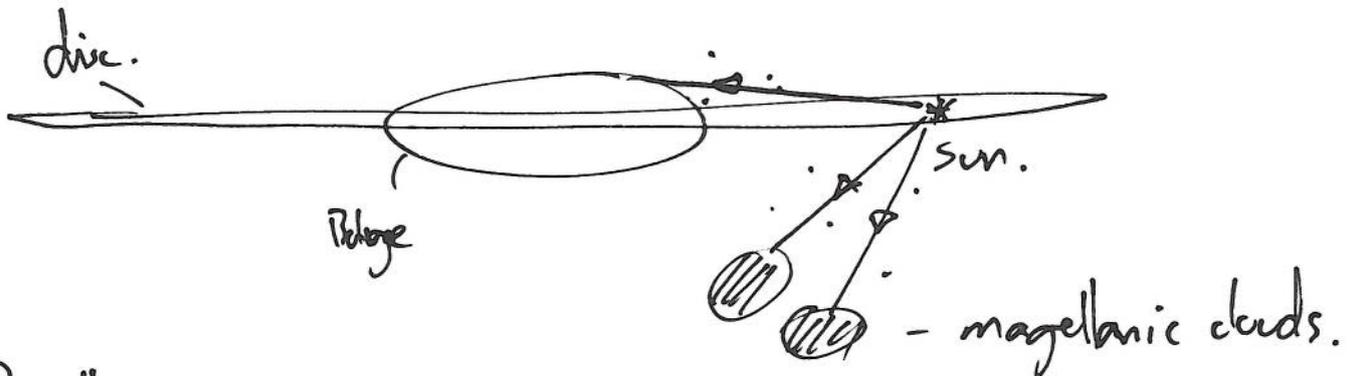
Search for MACHOs via microlensing.



when perfectly aligned, gravitational lensing amplifies the brightness of a bgd. star.

→ C.R. in 4<sup>th</sup> yr.

microlensing surveys carried out in 1990s; observing in directions with many millions of bgd stars.



Results - 100s of events detected, duration of events sensitive to mass  $\Rightarrow \bar{m} \sim 0.5 M_{\odot}$   
 $\Rightarrow$  white dwarf stars.

But, only see enough events to account for 14.11.3  
 $\leq 2\%$  of dark matter in these regions.

Additional evidence from the abundance ratios of elements & isotopes from the big bang (Big Bang Nucleosynthesis) which suggests dark matter cannot be baryonic.

→ 3<sup>rd</sup> yr cosmology.

3<sup>rd</sup> alternative, that dark matter doesn't exist, and is inferred through relying on incorrect theories of gravity, e.g. modified Newtonian gravity dynamics MOND,  $F_g \propto \frac{1}{R^2}$

---

### 3. Distances to galaxies

Need distances in order to measure all main properties:

→ size,  $R \approx \theta d$   
     $\theta$  angular size.

→ luminosity,  $L = \int_{L_{\text{min}}} 4\pi d^2$