

Heavy flavour physics

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- Plan
 - Kaon physics and SM construction (bit of history)
 - Establishing SM experimentally
 - Looking for breakdown of SM
- I have here more material than can be covered in four lectures, feel free to stop me if I'm explaining obvious

Outline – Chapter 1

- What is flavour physics and what is not
- Kaon physics – understand its importance for development of standard model of particle physics
 - Weak decays – quark mixing
 - FCNC kaon decays – GIM mechanism
 - Neutral kaon mixing
 - CP violation in neutral kaons
 - How to accommodate CP violation to model

Content of standard model

Fermions
("matter")

Bosons
("forces")

$$\left\{ \begin{array}{l} \text{Quarks} \\ uu\bar{u} \quad cc\bar{c} \quad tt\bar{t} \\ dd\bar{d} \quad ss\bar{s} \quad bb\bar{b} \\ \\ \text{Leptons} \\ e \quad \mu \quad \tau \\ \nu_e \quad \nu_\mu \quad \nu_\tau \end{array} \right\} \times \left\{ \begin{array}{l} \text{MATTER} \\ \text{ANTIMATTER} \end{array} \right\}$$

$gggggggg$

γ

W^+

W^-

Z

H

Parameters of standard model

- 3 gauge couplings
- 2 Higgs parameters
- 6 quark masses
- 3 quark mixing angles + 1 phase
- 3 (+3) lepton masses
- (3 lepton mixing angles + 1 phase)
- Why 3 generations (are we sure about it)?
- Why hierarchy in mass?
- Why hierarchy in mixing?
- Why do we have only matter in current Universe?

Flavour parameters

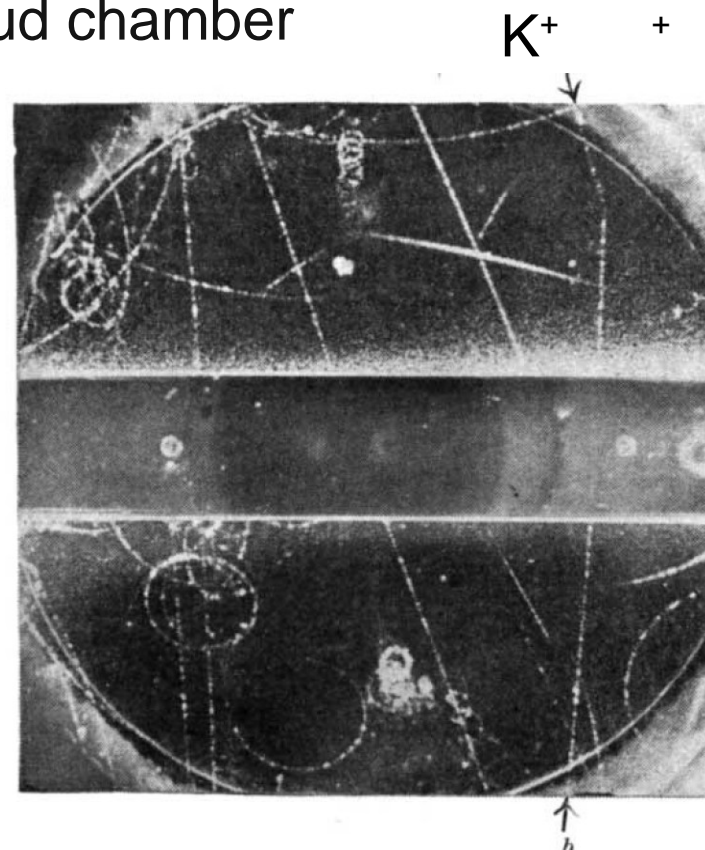
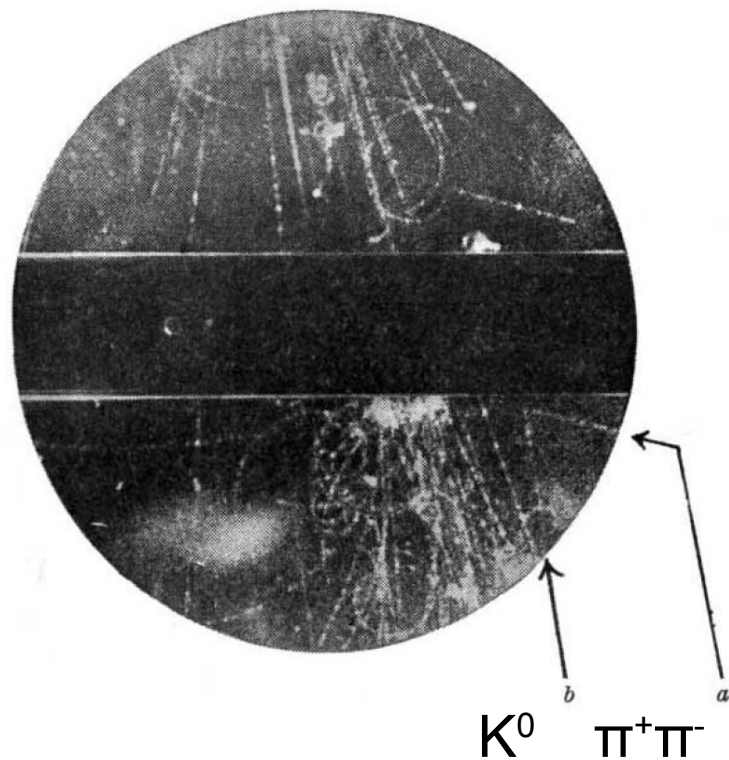
What is not flavour physics

- QCD: Strong interactions
 - Any details of QCD including studies of different “exciting” states
- Electroweak physics
 - There is some relation, but questions do not overlap
- Energy frontier
 - Search for new particles in production (on-shell)

Going to history
But explaining lot of things

Kaon discovery

- 1947, G. D. Rochester and C. C. Butler
- Using “fancy” detector called cloud chamber



- Produced in strong interaction
- Decay rather slow, lifetime of $10^{-8} - 10^{-10}$ s

Quark mixing - Cabibbo

- Quark content of kaon is $u\bar{s}$ (K^+) and $d\bar{s}$ (K^0)
- Main decays are
 - $K^+ \rightarrow \mu^+ \nu_\mu$, $K^+ \rightarrow \pi^0 e^+ \nu_e$, $K^0 \rightarrow \pi\pi$
 - Weak interaction has to allow transition $s \rightarrow u$
- There are good reasons why W (weak interaction) couples only to left-handed doublets
 - How to construct doublets to allow $s \rightarrow u$ and $d \rightarrow u$?
- Cabibbo provided solution in terms of quark mixing
- Doublet of weak interaction is $(u, d') = (u, d \cos(\theta) + s \sin(\theta))$
- θ is quark mixing angle, which was determined experimentally
- Actually solved difference in G between nuclear and muon decay

- Next piece of puzzle comes from FCNC kaon decays
- Cabibbo fixed one issue ($s \rightarrow u$ transition), but introduced another one
- If doublet of weak interaction is (u, d') , then also Z^0 can couple to $d' \bar{d}'$
- What does it mean in terms of original quarks?

$$u\bar{u} + d\bar{d} \cos^2 \theta + s\bar{s} \sin^2 \theta + (s\bar{d} + \bar{s}d) \sin \theta \cos \theta$$
- First three terms are fine, but last part causes problem
- It would allow flavour changing neutral current decays at tree-level
 - $K^+ \rightarrow \pi^+ e^+ e^-$ would be approximately 5% of $K^+ \rightarrow \pi^0 e^+ \nu_e$
 - But in experiment it was known to be $< 10^{-5}$

- Is Cabibbo wrong, or can we find some way to fix it?
- Not quite with three quarks known at the time, but
- In 1970 Glashow, Iliopoulos, Maiani suggested way
- To existing doublet $(u, d') = (u, d \cos(\theta) + s \sin(\theta))$ add second one
 $(c, s') = (c, d \cos(\theta) - s \sin(\theta))$
- Now Z^0 would also couple to $s' \bar{s}'$ which would give us term like
 $-(\bar{s}d + \bar{s}d) \sin\theta \cos\theta$ which cancels contribution from other doublet
 - Cancellation not perfect due to other contributions
- So in 1970 charm quark was predicted, despite that not everybody accepted existence of the quarks

Neutral Kaon Oscillation

- Now we come to next puzzle about neutral kaon lifetimes
- Originally two particles were seen with same mass, but very different lifetimes $9 \cdot 10^{-11}$ s and $5 \cdot 10^{-8}$
- They not only have very different lifetimes, but first one decays to 2π while other to 3π
- Both were produced in same type of interaction in association with other strange particles
- Is this just strange coincidence or is there something more behind it?
- Different decays suggest that lifetimes have something to do with CP symmetry

- To explain different lifetimes, let's look to CP properties
 - $CP | 2\pi \rangle = + | 2\pi \rangle$
 - $CP | 3\pi \rangle = - | 3\pi \rangle$
- Shorter lived kaon (call it $|K_1\rangle$) decays to 2π and is CP-even
- Longer lived kaon (call it $|K_2\rangle$) decays to 3π and is CP-odd
- Difference in the lifetimes come from different phase space available in two decays
 - $m(2\pi)=279$ MeV, $m(3\pi)=419$ MeV and $M(K^0)=497$ MeV

$$d\Gamma = \frac{(2\pi)^4}{2M} |M|^2 d\Phi_n \quad d\Phi_n = \delta^4(P - \sum p_i) \prod \frac{d^3 p_i}{(2\pi)^3 2E_i}$$

Neutral kaon mixing

- Now we have to put together fact that in strong interaction we produce K^0 or \bar{K}^0 , while in weak interaction (decay) we have K_1 and K_2
- But we already know from quark mixing, that quarks entering strong and weak interaction are not exactly same
- So we can connect kaons from strong interaction to those in weak interaction via mixing
- We can define those as
 - $K_1 = 1/2(K^0 + \bar{K}^0)$
 - $K_2 = 1/2(K^0 - \bar{K}^0)$
 - With CP $|K^0\rangle = +\bar{K}^0$ and CP $|\bar{K}^0\rangle = +K^0$ all fits together

Time evolution

- Now we can start to look to time evolution
- Definitely one set of states will behave like $e^{(\Gamma/2+im)t}$
- Question is which ones behave this way?
- After deciding above question, it is easy to calculate what to expect at given time for all four states
- There is interesting effect called kaon regeneration which we have no time to discuss here, but it is useful to understand it

Blackboard is my friend here

$K^0 - \bar{K}^0$ oscillation

$$|K_1\rangle = |K_1(0)\rangle e^{(-\frac{\Gamma_1}{2} + im_1)t}$$

$$|K_2\rangle = |K_2(0)\rangle e^{(-\frac{\Gamma_2}{2} + im_2)t}$$

$$|K_1(0)\rangle =$$

$$|K_0\rangle = \frac{1}{\sqrt{2}} (|K_1\rangle + |K_2\rangle)$$

$$+ : \langle K^0(t) | K^0(t) \rangle$$

$$\frac{1}{2} \left(\langle K_1^* | K_1 \rangle + \langle K_2^* | K_2 \rangle + \langle K_1^* | K_2 \rangle + \langle K_2^* | K_1 \rangle \right)$$

$$\downarrow \quad \downarrow$$

$$e^{-\Gamma_1 t} + e^{-\Gamma_2 t} + e^{(-\frac{\Gamma_1}{2} - im_1)t} e^{(-\frac{\Gamma_2}{2} + im_2)t}$$

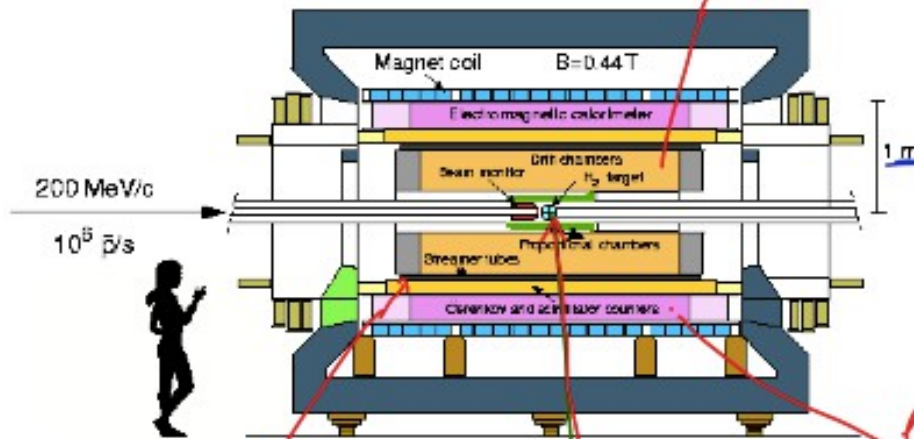
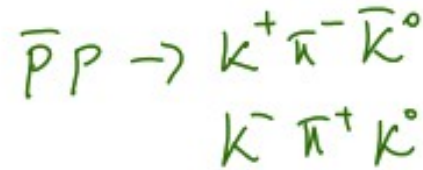
$$e^{(-\frac{\Gamma_2}{2} - im_2)t} e^{(-\frac{\Gamma_1}{2} + im_1)t}$$

$$\bar{K}^0 : e^{-\Gamma_1 t} + e^{-\Gamma_2 t} - \cos(m_2 - m_1)t e^{-\frac{\Gamma_1 + \Gamma_2}{2} t} \left[e^{-i(m_1 - m_2)t} + e^{-i(m_2 - m_1)t} \right]$$

R

CPLEAR experiment

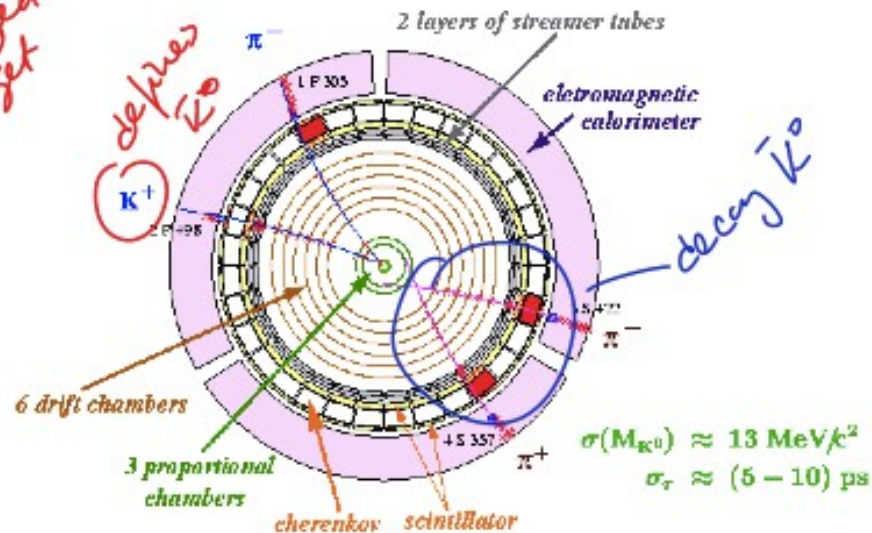
at CERN
 cplear.web.cern.ch



EM Calorimeter

Particle ID
 TOF, dE/dx,
 Cherenkov detector

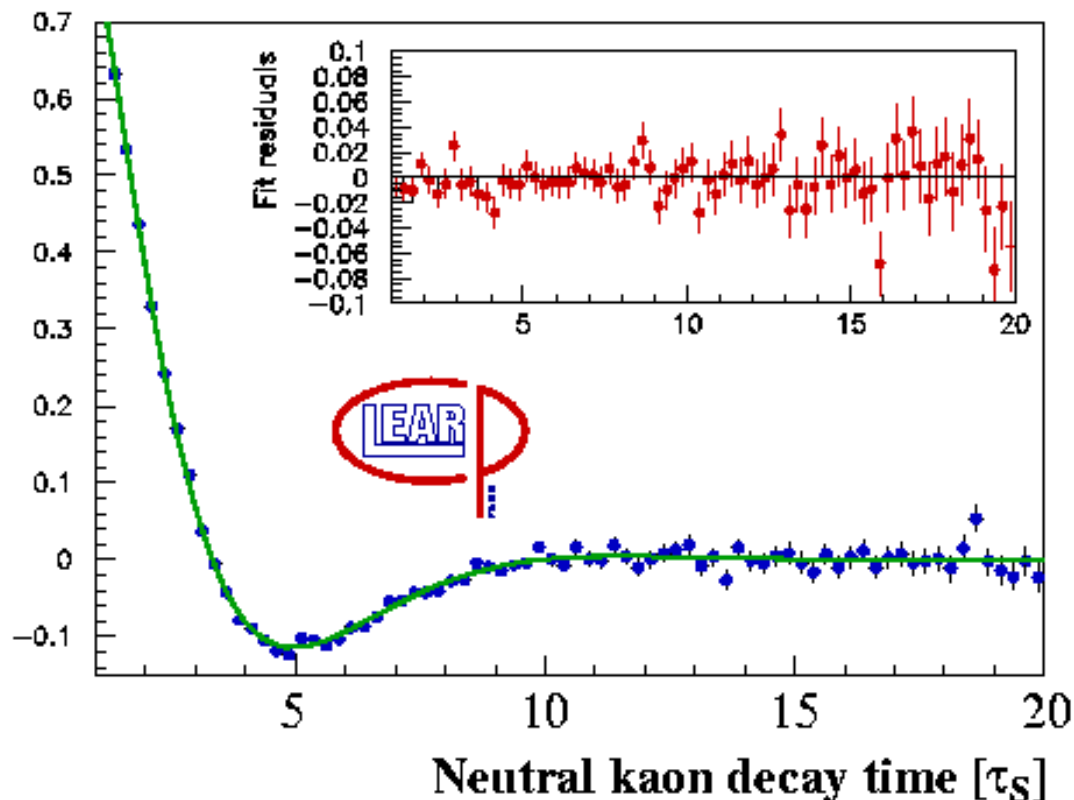
Hydrogen
 target



$$\sigma(M_{K^0}) \approx 13 \text{ MeV}^2$$

$$\sigma_r \approx (5 - 10) \text{ ps}$$

Kaon mixing in experiment



$$R_+(\tau) = R(K^0_{\tau=0} \rightarrow e^+\pi^-\nu)$$

$$\bar{R}_-(\tau) = R(\bar{K}^0_{\tau=0} \rightarrow e^-\pi^+\bar{\nu})$$

$$R_-(\tau) = R(K^0_{\tau=0} \rightarrow e^-\pi^+\bar{\nu})$$

$$\bar{R}_+(\tau) = R(\bar{K}^0_{\tau=0} \rightarrow e^+\pi^-\nu)$$

$$A_{\Delta m} = \frac{R_+ + \bar{R}_- - R_- + \bar{R}_+}{R_+ + \bar{R}_- + R_- + \bar{R}_+}$$

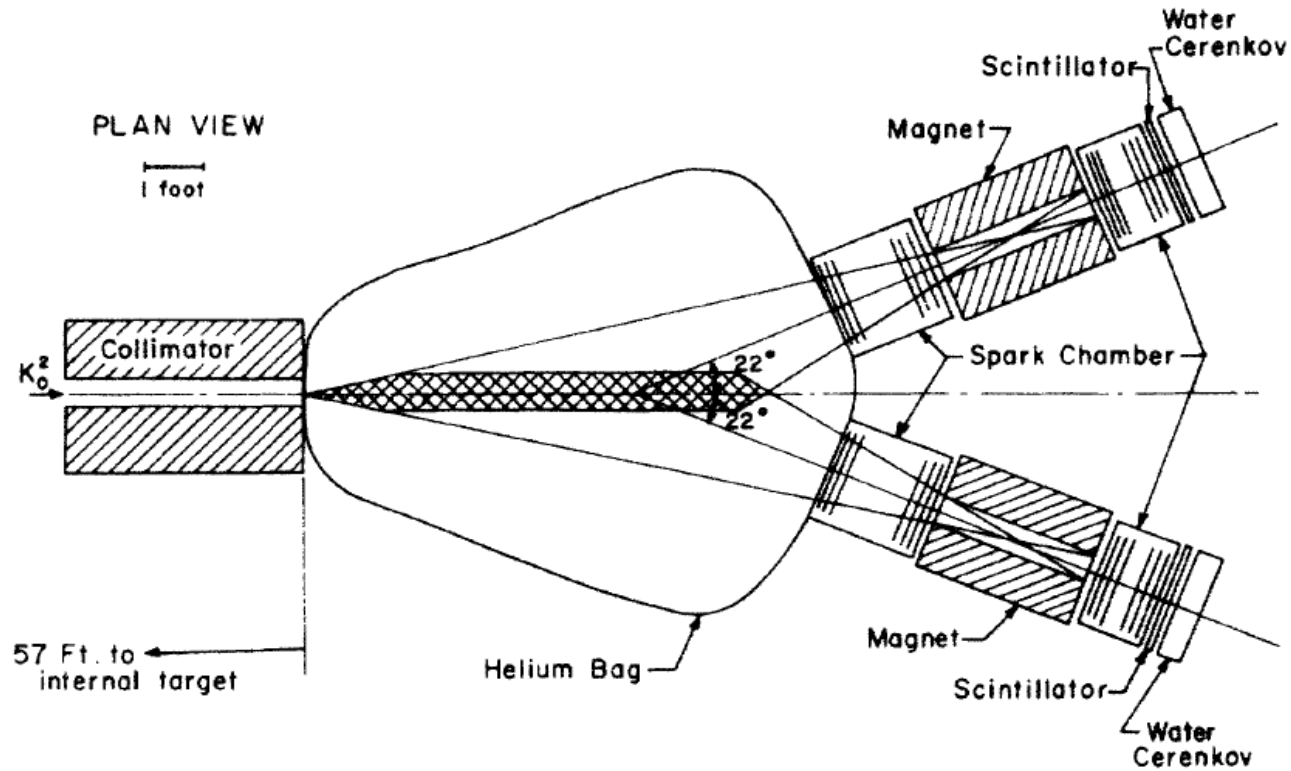
$$= 2 \frac{e^{-1/2(1/\tau_S + 1/\tau_L)\tau} \times \cos(\Delta m \cdot \tau)}{[1 + 2\Re(x_+)] e^{-\tau/\tau_S} + [1 - 2\Re(x_+)] e^{-\tau/\tau_L}}$$

- Gives $\Delta M = 529 \cdot 10^{-7} \text{ s}^{-1}$

CP Violation

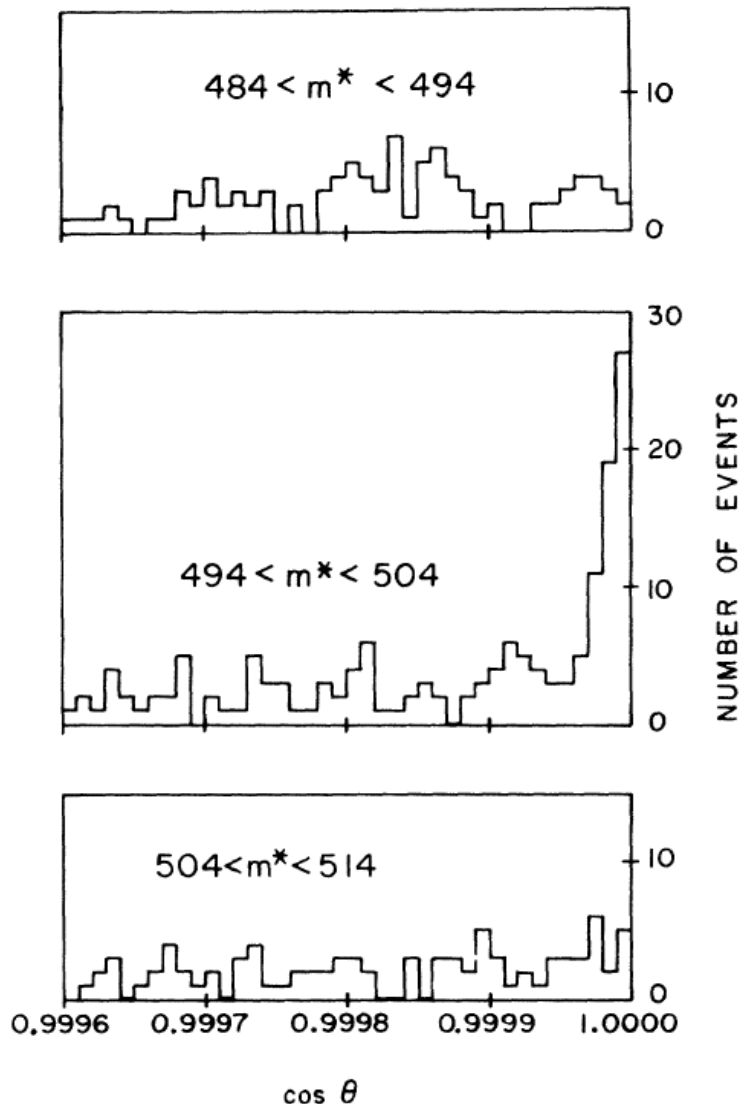
- We defined K_1 to be CP-even and K_2 CP-odd
- If CP is conserved, then
 - K_1 decays only to 2π
 - K_2 decays only to 3π
- What happens when CP is violated?
- Could we experimentally test CP violation?

Experimental test of CPV



Christenson, Cronin, Fitch, Turley

Result of the experiment



- If CP is violated, should see $K_2 \rightarrow 2\pi$
- Angle between sum of the momenta of 2π and beam should be zero
- Experiment measured

$$R = \frac{N(K_2 \rightarrow \pi^+ \pi^-)}{N(K_2 \rightarrow \text{all charged})} = (2 \pm 0.4)10^{-3}$$

How to make sense out of it?

→ K_1, K_2 are not eigenstates of weak inter.

$$K_S = \frac{1}{\sqrt{1+|\varepsilon|^2}} (K_1 + \varepsilon K_2) = \frac{1}{\sqrt{2(1+|\varepsilon|^2)}} \left[(1+\varepsilon)K^0 + (1-\varepsilon)\bar{K}^0 \right]$$

$$K_L = \frac{1}{\sqrt{1+|\varepsilon|^2}} (K_2 + \varepsilon K_1) \approx K_2$$

$\Gamma(K_1 \rightarrow 2\pi) \sim \frac{1}{\tau_1}$

$$\Gamma(K_L \rightarrow 2\pi) \approx \varepsilon^2 A^2 \Gamma(K_1 \rightarrow 2\pi) \approx \varepsilon^2 \frac{1}{\tau_1}$$

$$\xi^2 = R_{\pm} \frac{\tau_1}{\tau_2}$$

$$\Gamma(K_L \rightarrow 2\pi) \sim \underbrace{\frac{\Gamma(K_L \rightarrow 2\pi)}{\Gamma(K_L \rightarrow \text{all})}}_R \cdot \Gamma(K_2 \rightarrow \text{all}) \sim \frac{1}{\tau_2}$$

$$R_{\pm} = \frac{3}{2} R$$

$$\xi = 2.3 \times 10^{-3}$$

Example of $K_L \rightarrow e^+ \pi^- \nu$

$$\Delta = \frac{N(K_L \rightarrow e^+ \pi^- \nu) - N(K_L \rightarrow e^- \pi^+ \nu)}{N(K_L \rightarrow e^+ \pi^- \nu) + N(K_L \rightarrow e^- \pi^+ \nu)} \quad \leftarrow \text{Num}$$

$$\text{Num} = (1+\epsilon) \cancel{[K^0 \rightarrow \bar{u}^+ e^- \bar{\nu}]} + (1-\epsilon) [\bar{K}^0 \rightarrow \bar{u}^+ e^- \bar{\nu}] - (1+\epsilon) [K^0 \rightarrow \bar{u}^- e^+ \nu] - \cancel{(1-\epsilon) [\bar{K}^0 \rightarrow \bar{u}^- e^+ \nu]}$$

assume $\bar{K}^0 \rightarrow \bar{u}^+ e^- \bar{\nu} = K^0 \rightarrow \bar{u}^- e^+ \nu$

$$\text{Num} = -2\epsilon R(K^0 \rightarrow \bar{u}^- e^+ \nu)$$

$$\Delta = 2 \text{Re}(\epsilon)$$

Experiment

$$\Delta_e = 3.34 \times 10^{-3}$$
$$\Delta_\mu = 3.04 \times 10^{-3}$$

Indirect CPV

$$|\psi\rangle = p |K^0\rangle + q |\bar{K}^0\rangle$$

p, q - complex numbers
 $|p|^2 + |q|^2 = 1$

$$\begin{pmatrix} p \\ q \end{pmatrix}$$

Schrödinger type eq.

$$i \frac{d}{dt} |\psi\rangle = \left[\begin{pmatrix} M_{11} & M_{12} \\ M_{12}^* & M_{22} \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma_{22} \end{pmatrix} \right] |\psi\rangle$$

M_{ij} are hermitian matrices

mass matrix
 \Rightarrow oscillation

decay matrix
 \Rightarrow decay

eigenstates, eigenvalues

$$\left(\frac{q}{p}\right)^2 = \frac{M_{12}^* - \frac{i}{2} \Gamma_{12}^*}{M_{12} - \frac{i}{2} \Gamma_{12}}$$

if $|q| = |p| \Rightarrow M_{12}^* - \frac{i}{2} \Gamma_{12}^* = M_{12} - \frac{i}{2} \Gamma_{12} \Rightarrow$ zero phase between M_{12} and Γ_{12}

Standard model

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \cdot \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

Kobayashi
Maskawa

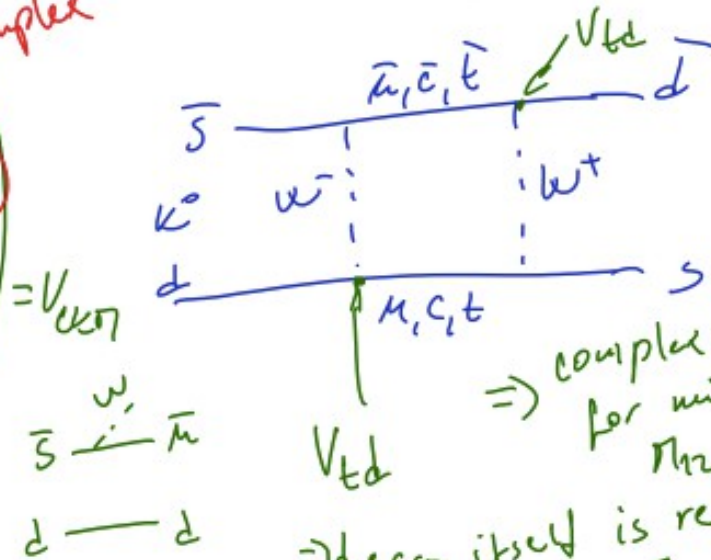
proposed third generation
of quarks

⇒ parametrized by 3 rotations and
1 complex phase

Wolfenstein parametrization

$$\begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} = V_{CKM}$$

complex



⇒ complex phase
for mixing
the
real

⇒ decay itself is real
 η real

$$\lambda = \sin \theta_C \approx 0.22$$

Note on CKM matrix

- CKM matrix is unitary matrix
- It has only four parameters
- Product of any two rows or two columns is equal to zero
 - It can be visualized as triangle in complex plain (called unitarity triangle)
- All unitarity triangles have same area given by Jarlskog invariant
- Jarlskog invariant is measure of CP violation in quark sector
- The CKM matrix is hierarchical



Some questions for thinking

- What are implications of observation of CP violation?
- What you would do to confirm Kobayashi-Maskawa mechanism
- If you have answers in terms of experiment, what capabilities experiment has to have?
- How would you determine CKM matrix elements?