

# Quark Flavour Physics

1. Draw Feynman diagrams for decays  $\pi^- \rightarrow \mu^- \bar{\nu}_\mu$  and  $K^- \rightarrow \mu^- \bar{\nu}_\mu$ . The branching fractions of two are measured to be  $\mathcal{B}(\pi^- \rightarrow \mu^- \bar{\nu}_\mu) = 0.999877 \pm 0.0000004$  and  $\mathcal{B}(K^- \rightarrow \mu^- \bar{\nu}_\mu) = 0.6355 \pm 0.0011$ . Decay rate of each decay is given by

$$\Gamma = |V_{uq}|^2 G_F^2 f_p^2 m_p m_\mu^2 (1 - m_\mu^2/m_p^2)^2 \quad (1)$$

where  $f_\pi = (130.41 \pm 0.03 \pm 0.20) \text{ MeV}$ ,  $f_K = (156.1 \pm 0.2 \pm 0.8 \pm 0.2) \text{ MeV}$  with masses being  $m_\mu = 105.7 \text{ MeV}$ ,  $m_\pi = 139.57 \text{ MeV}$  and  $m_K = 493.7 \text{ MeV}$  and lifetimes being  $\tau(\pi^+) = 2.6033 \times 10^{-8} \text{ s}$  and  $\tau(K^+) = 1.2385 \times 10^{-8} \text{ s}$ . Using this estimate Cabbibo angle.

2. Consider pure beam of long lived neutral kaons. As the  $K^0$  and  $\bar{K}^0$  interaction cross section with matter leads to interesting effect known as kaon regeneration. Essence of it is that after pure  $K_2$  beam traverse block of matter, it contains again  $K_1$  component. Denoting  $K^0$  integrated cross section with block of matter as  $f$  and  $\bar{K}^0$  as  $\bar{f}$  find out amount of  $K_2$  and  $K_1$  component after pure  $K_2$  beam traverses given block of matter.
3. Using discussed formalism, verify that  $K_L \rightarrow 2\pi$  rate is indeed proportional to  $\epsilon$ .
4. Neutral meson mixing is described by equation

$$i \frac{d}{dt} \begin{pmatrix} |B_s(t)\rangle \\ |\bar{B}_s(t)\rangle \end{pmatrix} = \left( \hat{M} - \frac{i}{2} \hat{\Gamma} \right) \begin{pmatrix} |B_s(t)\rangle \\ |\bar{B}_s(t)\rangle \end{pmatrix}.$$

Diagonalization leads to eigenstates with definite masses and lifetimes

$$\begin{aligned} |B_{sH}^0\rangle &= p |B_s\rangle + q |\bar{B}_s\rangle, \\ |B_{sL}^0\rangle &= p |B_s\rangle - q |\bar{B}_s\rangle, \end{aligned}$$

with  $p$  and  $q$  being complex numbers satisfying  $|p|^2 + |q|^2 = 1$ . Diagonalise matrix and find two mass states.

5. Which of the following decays can show  $CP$  violation in standard model. Draw Feynman diagrams and decide which type of  $CP$  violation. Decays to exhibit are:
  - (a)  $D^0 \rightarrow K^+ K^-$
  - (b)  $B^+ \rightarrow J/\psi K^+$
  - (c)  $B^0 \rightarrow J/\psi \rho$
  - (d)  $B_s^0 \rightarrow \phi \phi$
  - (e)  $B^0 \rightarrow K^+ \pi^-$

- (f)  $B^+ \rightarrow [\pi^+\pi^-]_D K^+$  where  $[\pi^+\pi^-]_D$  is combination of two pions consistent with originating from  $D^0$  or  $\bar{D}^0$ .
  - (g)  $B^+ \rightarrow [\pi^+\pi^-]_D K^-$
  - (h)  $\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^-$
  - (i)  $\Lambda_b^0 \rightarrow \Lambda \pi^+ \pi^-$
6. What are differences in flavour tagging between  $e^+e^-$  machines at  $\Upsilon(4S)$  energies and hadron colliders.
  7. List physics sources of imperfection of flavour tagging. Consider also differences between  $e^+e^-$  machines at  $\Upsilon(4S)$  energies and hadron colliders.
  8. Why low energy  $e^+e^-$  colliders cannot compete with hadronic machines in studies of time evolution of  $B_s$ .
  9. Imagine that there is a fourth family of quarks  $(t', b')$  with  $m(t') > m(b')$ , that is decoupled from the three SM families since  $V_{t'b'} = 1$ . Describe how the  $b'$  quark might be detected. If a strongly bound  $b'b'$ bar state exists, would it decay and if so, how?
  10. Draw a Feynman diagram for the leptonic decay  $D_s^+ \rightarrow \mu^+ \nu$ . What property of the CKM matrix can be determined from the measurement of its branching fraction?
  11. Draw a Feynman diagram for the rare decay  $K_L \rightarrow \pi^0 \nu \bar{\nu}$ . What property of the Unitarity Triangle can be determined from the measurement of its branching fraction?