# APTS Statistical Modelling: Practical 1 

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The code below generates a time series of length $n$, and then fits autoregressive models of order up to order.max, which is 20 below. The function AIC is plotted as a function of the order, and the optimal order is tabulated. ${ }^{1}$

```
plot.aic <- function(fit, new=T, sd=0.1)
{ # code to plot AIC against order of AR model fitted
if (new) plot((1:length(fit$aic))-1,fit$aic,type="l",xlab="Order",ylab="AIC") else
        lines((1:length(fit$aic))-1,fit$aic,type="l")
    points(rnorm(1,fit$order,sd=sd),rnorm(1,sd=sd),pch=16,col="red")
}
# generates data from an autoregressive process, by default of order 1
sim.y <- function(n, model=list(ar=c(0.9))) arima.sim(model=model, n)
n <- 20 # length of time series
R <- 1000 # number of replicates
# first dataset to get things started
y <- sim.y(n)
fit <- ar(y,order.max=19)
plot.aic(fit)
# we will store the orders chosen using AIC, BIC, and AICC
AIC.order <- NULL
BIC.order <- NULL
AICC.order <- NULL
# Now make R replicates, plot the corresponding AIC curves
for (i in 1:R )
{
fit <- ar( sim.y(n, model=list(ar=c(0.5,0.1))) )
plot.aic(fit, new=F)
AIC.order <- c(AIC.order, fit$order)
# The next two lines should be uncommented and modified to give the
# optimal orders when BIC and AICC are used for order selection
# BIC.order <- c(BIC.order, NA)
# AICC.order <- c(AICC.order, NA)
}
# tabulate the order of the chosen model
table(AIC.order)
```

[^0](a) Try seeing how AIC performs as a basis for model selection for $n=20,50,100,500$.
(b) Vary the simulation model, using, for example, the model=list (ma=0.9) in the arima.sim function, to see how well AIC works when the data are not generated by an autoregressive model.
(c) Modify the code above to compute the values of BIC and $\mathrm{AIC}_{\mathrm{c}}$, where
$$
\mathrm{AIC}=2(p+1-\widehat{\ell}), \quad \mathrm{BIC}=p \log n-2 \widehat{\ell}, \quad \mathrm{AIC}_{\mathrm{c}}=n \frac{n+p}{n-p-2}-2 \widehat{\ell}
$$
where $p$ is the order of the fitted model, and assess how well they perform as bases for model selection, for $n=20,50,100,500$.


[^0]:    ${ }^{1}$ The code is available from the APTS website.

