## APTS Statistical Modelling: Practical 1

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The code below generates a time series of length n, and then fits autoregressive models of order up to order.max, which is 20 below. The function AIC is plotted as a function of the order, and the optimal order is tabulated.<sup>1</sup>

```
plot.aic <- function(fit, new=T, sd=0.1)</pre>
{ # code to plot AIC against order of AR model fitted
if (new) plot((1:length(fit$aic))-1,fit$aic,type="l",xlab="Order",ylab="AIC") else
         lines((1:length(fit$aic))-1,fit$aic,type="l")
    points(rnorm(1,fit$order,sd=sd),rnorm(1,sd=sd),pch=16,col="red")
}
# generates data from an autoregressive process, by default of order 1
sim.y <- function(n, model=list(ar=c(0.9))) arima.sim(model=model, n)</pre>
n <- 20 # length of time series
R <- 1000 # number of replicates
# first dataset to get things started
y \leftarrow sim.y(n)
fit <- ar(y,order.max=19)</pre>
plot.aic(fit)
# we will store the orders chosen using AIC, BIC, and AICC
AIC.order <- NULL
BIC.order <- NULL
AICC.order <- NULL
# Now make R replicates, plot the corresponding AIC curves
for (i in 1:R)
fit \leftarrow ar( sim.y(n, model=list(ar=c(0.5,0.1))) )
plot.aic(fit, new=F)
AIC.order <- c(AIC.order, fit$order)
# The next two lines should be uncommented and modified to give the
# optimal orders when BIC and AICC are used for order selection
# BIC.order <- c(BIC.order, NA)
# AICC.order <- c(AICC.order, NA)
}
# tabulate the order of the chosen model
table(AIC.order)
```

<sup>&</sup>lt;sup>1</sup>The code is available from the APTS website.

- (a) Try seeing how AIC performs as a basis for model selection for n = 20, 50, 100, 500.
- (b) Vary the simulation model, using, for example, the model=list(ma=0.9) in the arima.sim function, to see how well AIC works when the data are not generated by an autoregressive model.
- (c) Modify the code above to compute the values of BIC and AIC<sub>c</sub>, where

$$AIC = 2(p+1-\widehat{\ell}), \quad BIC = p\log n - 2\widehat{\ell}, \quad AIC_c = n\frac{n+p}{n-p-2} - 2\widehat{\ell},$$

where p is the order of the fitted model, and assess how well they perform as bases for model selection, for n = 20, 50, 100, 500.