

Emerging Geometries for Statistical Science: I. A Very Short Introduction

Look what geometry could do for you!

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 - orthogonal projection providing the necessary right-angle

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 - 3 *multinomial* geometry

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- *sensitivity analyses are sensible*

Let's see ...

What geometry could do for you! ...