

# ES2A7 - Fluid Mechanics Example Classes

## Example Questions (Set I)

### Question 1: Wind Tunnel

A simple wind-tunnel is depicted schematically in Figure 1. The flow speed in the working section is assumed to be constant with a value of  $V_B = 60\text{m/s}$  at point B. The cross-sectional area of the working section is  $1\text{ m}^2$ .

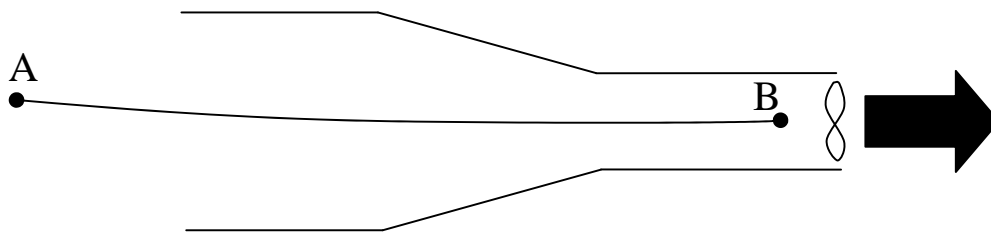


Figure 1: Sketch of simple wind-tunnel

- Neglecting irreversible losses, such as those due to viscous effects, calculate the gauge pressure in the working section. (Assume a value of  $\rho = 1.2\text{ kg/m}^3$  for the density of air).
- Calculate the mass flow rate across the cross-section in the working section.

### Question 2: Plunger

A plunger is moving through a cylinder as schematically illustrated in the Figure 2. The velocity of the plunger is  $V_p = 10\text{ ms}^{-1}$ . The oil film separating the plunger from the cylinder has a dynamic viscosity of  $\mu = 0.3\text{Nsm}^{-2}$ . Assume that the oil-film thickness is uniform over the entire peripheral surface of the plunger. Calculate the force and the power required to maintain this motion.

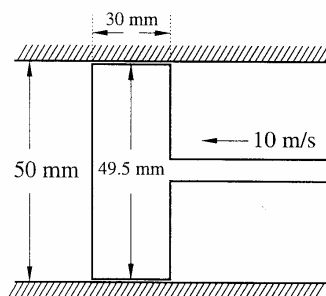


Figure 2: Plunger moving through cylinder.

### Question 3: Flow over Wing

Assume that a plane is flying with a constant velocity of  $v_0 = 55 \text{ ms}^{-1}$  at standard sea level conditions (Density air:  $\rho_0 = 1.23 \text{ kg m}^{-3}$ , Pressure:  $p_0 = 1.01 \times 10^5 \text{ Nm}^{-2}$ ). At some point on one of the plane's wings the pressure is measured as  $p = 0.95 \times 10^5 \text{ Nm}^{-2}$ . Calculate the flow velocity  $v$  at this point.

### Question 4: Sphere in Fluid

A sphere moves through oil. The constant velocity of the sphere is  $u = 1 \text{ mms}^{-1}$ . The dynamic viscosity of the oil is  $\mu = 0.05 \text{ Nsm}^{-2}$  and its density is  $\rho_o = 900 \text{ kgm}^{-3}$ . The radius of the sphere is  $r = 10 \text{ mm}$  and its density is  $\rho_s = 1200 \text{ kgm}^{-3}$ . (i) Use Figure 3 to estimate the drag forces acting on the sphere. (ii) Calculate the buoyancy force acting on the sphere.

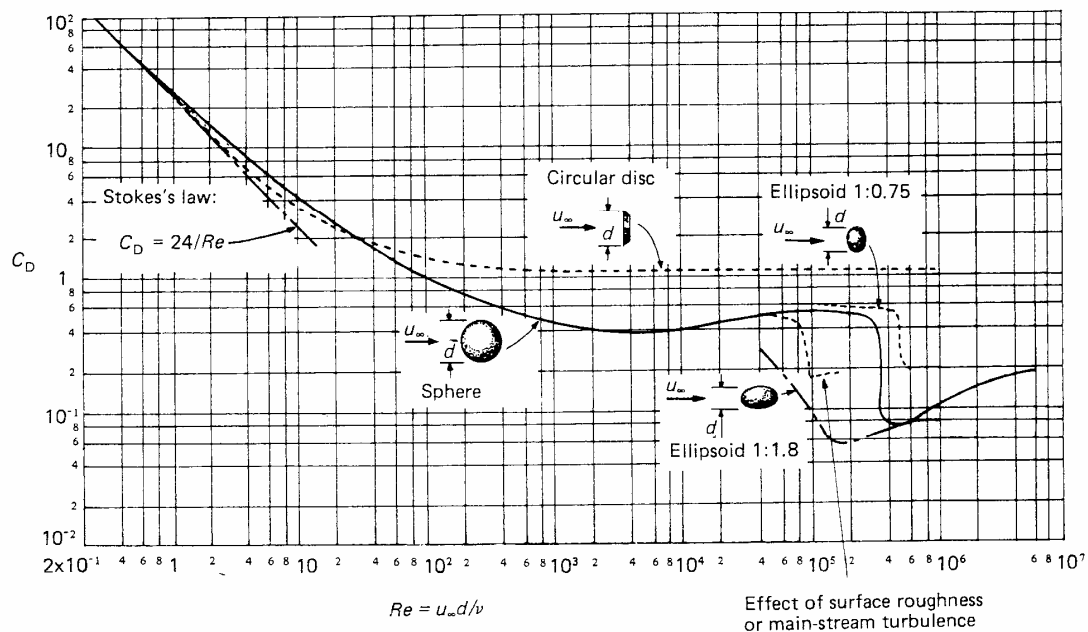


Figure 3: Drag coefficient of smooth, axially symmetric bodies (From: Massey, Mechanics of Fluids, Chapman & Hall, 1989, 6<sup>th</sup> Edition)

### Question 5: Fire Engine

A fire engine pump develops a head of 50 m, i.e. it increases the energy per unit weight of the water passing through it by  $50 \text{ N m N}^{-1}$ . The pump draws water from a sump at A (Fig. 4) through a 150 mm diameter pipe in which there is a loss of energy per unit weight due to friction  $h_1 = 5u_1^2/2g$  varying with the mean velocity  $u_1$  in the pipe, and discharges it through a 75 mm nozzle at C, 30 m above the pump, at the end of a 100 mm diameter delivery pipe in which there is a loss of energy per unit weight  $h_2 = 12u_2^2/2g$ . Calculate (a) the velocity of the jet issuing from the nozzle at C and (b) the pressure in the suction pipe at the inlet to the pump at B.

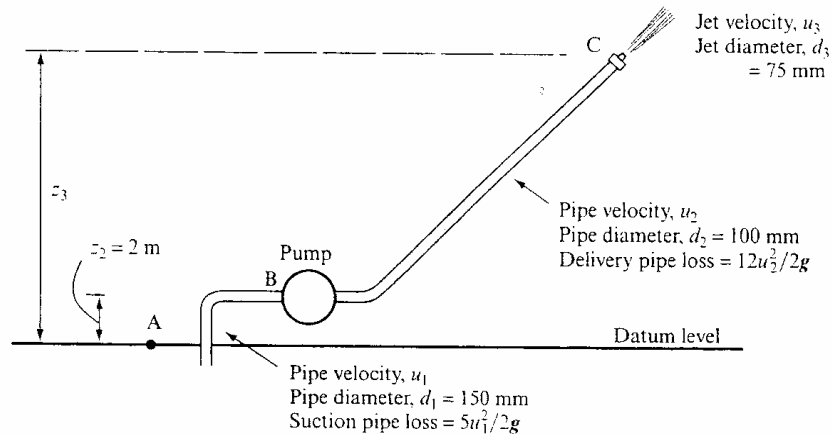


Figure 4: Fire engine Pump

### Question 6: Multi-Fluid Manometer

A multi-fluid manometer is set up as shown in Fig.5. The pressure at its right end is  $p_2 = 0.9 \times 10^5 \text{ Nm}^{-2}$ . The densities of the fluids are  $\rho_A = 1000 \text{ kg m}^{-3}$ ,  $\rho_B = 900 \text{ kg m}^{-3}$ ,  $\rho_C = 13000 \text{ kg m}^{-3}$ . One measures  $h_1 = 0.5 \text{ m}$ ,  $h_2 = 0.3 \text{ m}$  and  $h_3 = 0.6 \text{ m}$ . Find the pressure  $p_1$ .

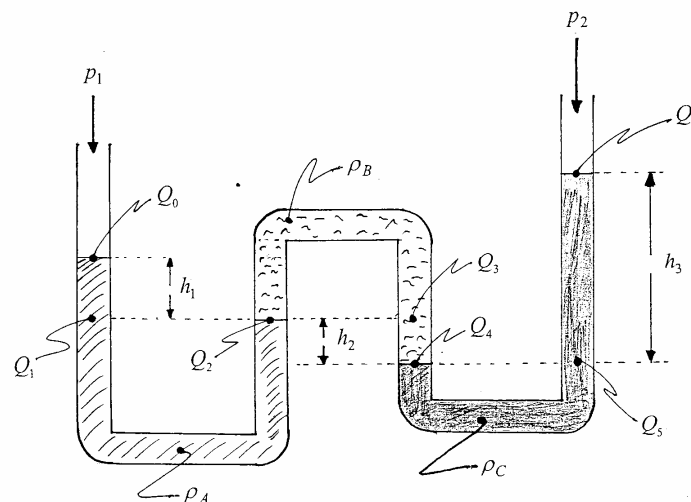


Figure 5: Multi-fluid manometer