

Q10.

BB, Bb, bb (0<sup>th</sup> generation)

$n \quad r \quad w \quad (n+r+w=1)$

[Hardy Weinberg principle]

$v = 2z$

1st generation

BB

$$n^2(1) + r^2\left(\frac{1}{4}\right) + w^2(0) + 2nw(0) + 2wr(0) + 2nr\left(\frac{1}{2}\right)$$

$$= (n+z)^2$$

$bb$   
 $(w+z)^2$

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Bb

$$n^2(0) + r^2\left(\frac{1}{4}\right) + w^2(0) + 2nw(1) + 2wr\left(\frac{1}{2}\right) + 2nr\left(\frac{1}{2}\right)$$

$$= 2(n+z)(w+z)$$


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R4.  $n+z+w=1$

$$(n+z+z+w)^2 = 1$$

$$\underbrace{(n+z)^2}_{BB} + \underbrace{(w+z)^2}_{bb} + 2(n+z)(w+z) = 1$$

$\therefore Bb$

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1<sup>st</sup> generation

BB      Bb      bb

$(n+z)^2 \quad 2(n+z)(w+z) \quad (w+z)^2$

0<sup>th</sup> generation

$n \quad 2z \quad w$

2<sup>nd</sup> generation

BB

$$\left( (n+z)^2 + (n+z)(w+z) \right)^2 = (n+z)^2$$

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Q5 iv)

BB Bb bb

brown blue

brown eyed woman, parents Bb

blue eyed man (bb)

$P(\text{woman has } b \mid \text{child is brown eyed}) = ?$

BB Bb woman is actually brown-eyed  $\frac{1}{4}$

$\frac{1}{4} \quad \frac{1}{2}$   $\frac{1}{4}$   $P(\text{woman BB}) = \frac{1/4}{1/4+1/2} = 1/3$

$\frac{1}{4}$   $\frac{1}{2}$   $\frac{1}{4}$   $P(\text{woman Bb}) = 2/3$

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$$\propto (n+z)^2 + (n+z)(w+z) : n+z$$

$$\propto n+z+w+z = 1$$

$n+z+z+w=1$  ✓

BB Bb bb (0<sup>th</sup> generation)

$$(n+z) \left[ (n+z) + (w+z) \right] = n+z$$

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$\frac{1}{3} \quad \frac{2}{3}$

BB Bb bb

Bb Bb bb

$\frac{1}{2} \quad \frac{1}{2}$

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Bayes' formula

$P(\text{mother has } Bb \mid \text{child brown eyed}) =$

$$\frac{P(CBE \mid M Bb) P(M Bb)}{P(CBE \mid M Bb) P(M Bb) + P(CBE \mid M BB) P(M BB)}$$

$$= \left( \frac{1}{2} \times \frac{2}{3} \right) / \left( \frac{1}{2} \times \frac{2}{3} + 1 \times \frac{1}{3} \right) = 1/2$$

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Comments.

Q5.

- interpret the sample points of  $\Omega$
- $\{(B_1, L), (B_1, L'), (B^c, L), (B^c, L')\}$
- $P(\underline{B_1, L}) = 0.05$  BAD notation!
- $\Omega = \{P(AB), P(A\bar{B}), \dots\}$  BAD notation!
- ✓  
tn. of these  $P$ -ties were the same!  
(two)

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Q3


- inclusion-exclusion principle  
+  
addition rule
- $(P(A) + P(B))^c$  X.

Q9. pairwise indep. vs. independence.

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Q5.

sampling with replacement  
vs.  
without

"  sample grows large so the difference between the two grows small. "

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